



Grand Challenge

UNIVERSITY OF COLORADO **BOULDER**

SPACE WEATHER CENTER

Satellite Drag: Aerodynamic Forces in LEO

*Marcin Pilinski
SWx-TREC*

LASP / University of Colorado

2018-04-25

*9th CCMC Community Workshop
College Park, Maryland*

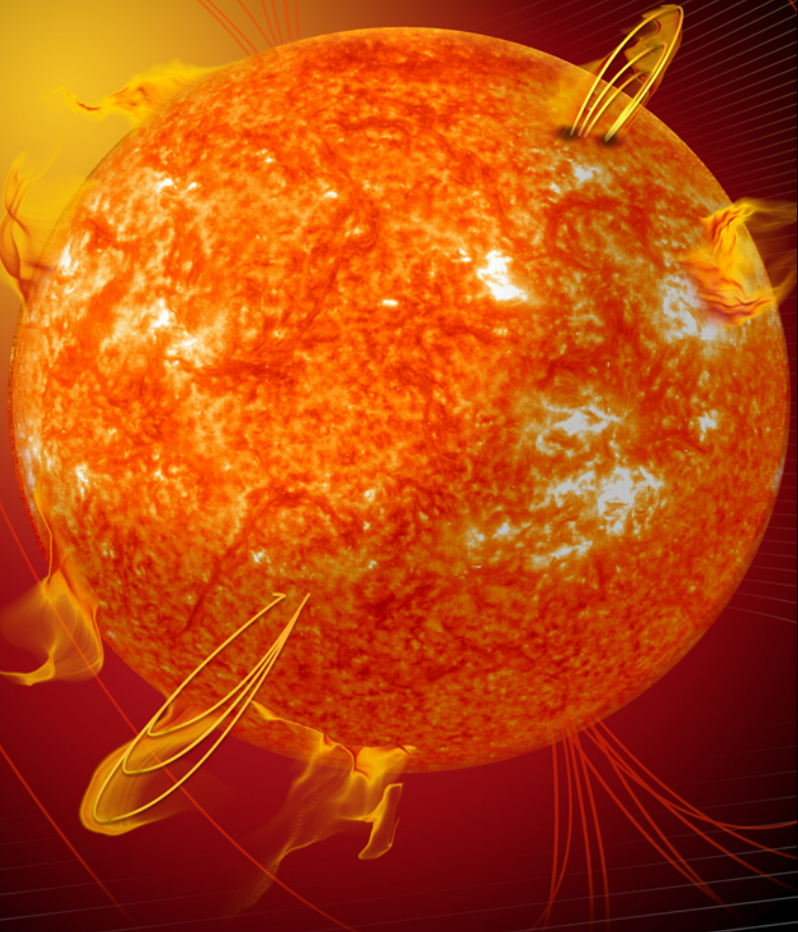




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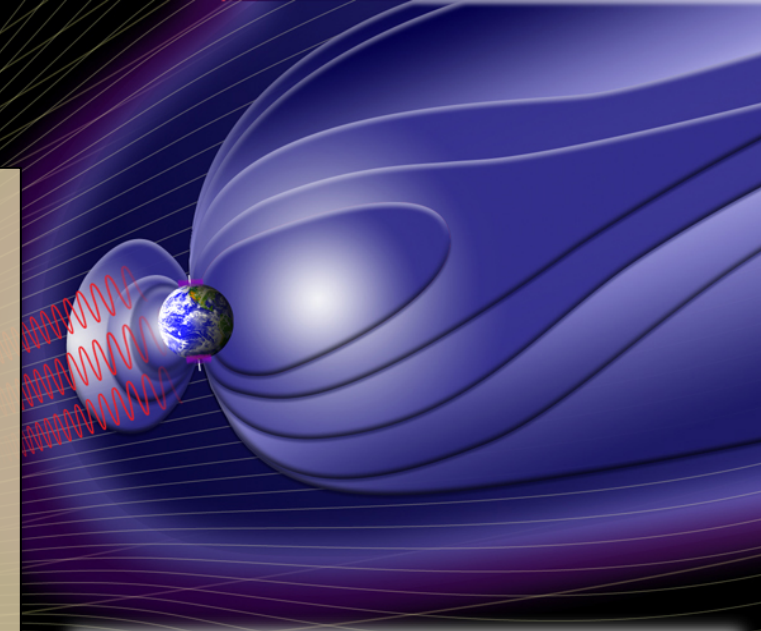
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SWx-TREC

Jeffrey P. Thayer, PI (AES), Tom Berger, Director (CEAS), Dan Baker (LASP), Steven Cranmer (APS), Chris Pankratz (LASP), Tim Fuller-Rowell (CIRES), Nils Halverson (APS), and Cora Randall (ATOC)

TREC is a new academic initiative to serve as a national center of excellence in cross-disciplinary research, technological innovation and education in space weather. As an academic endeavor, SWx TREC provides new pathways for federal agencies, academia, commercial partners and industry to collaboratively address the nation's evolving space weather forecasting, mitigation and response needs.

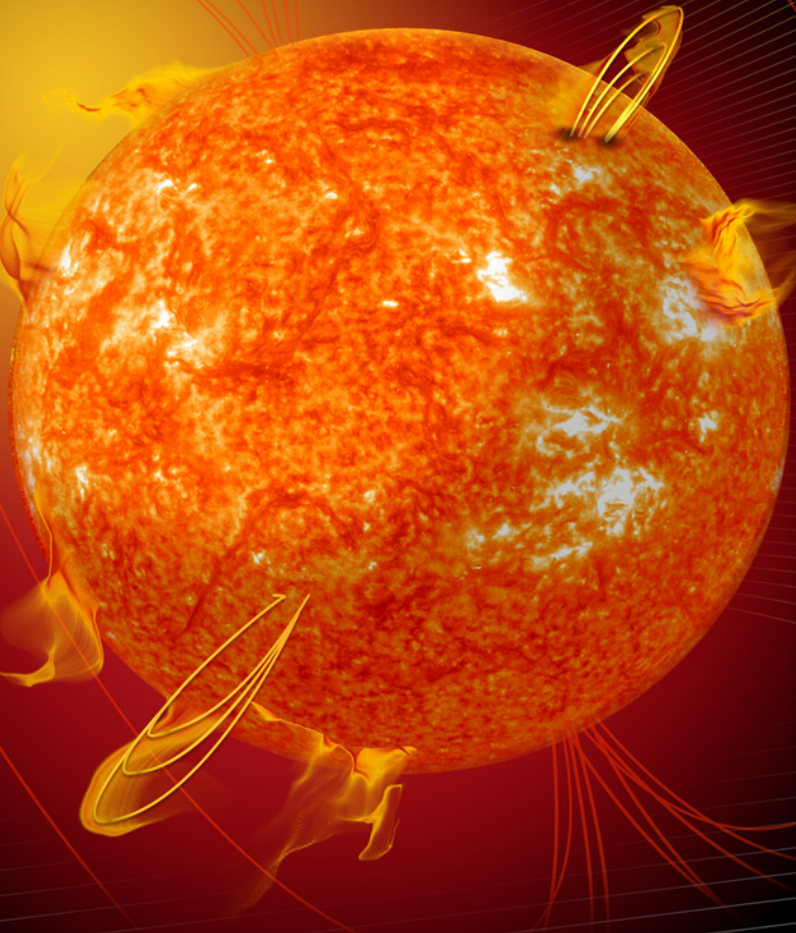




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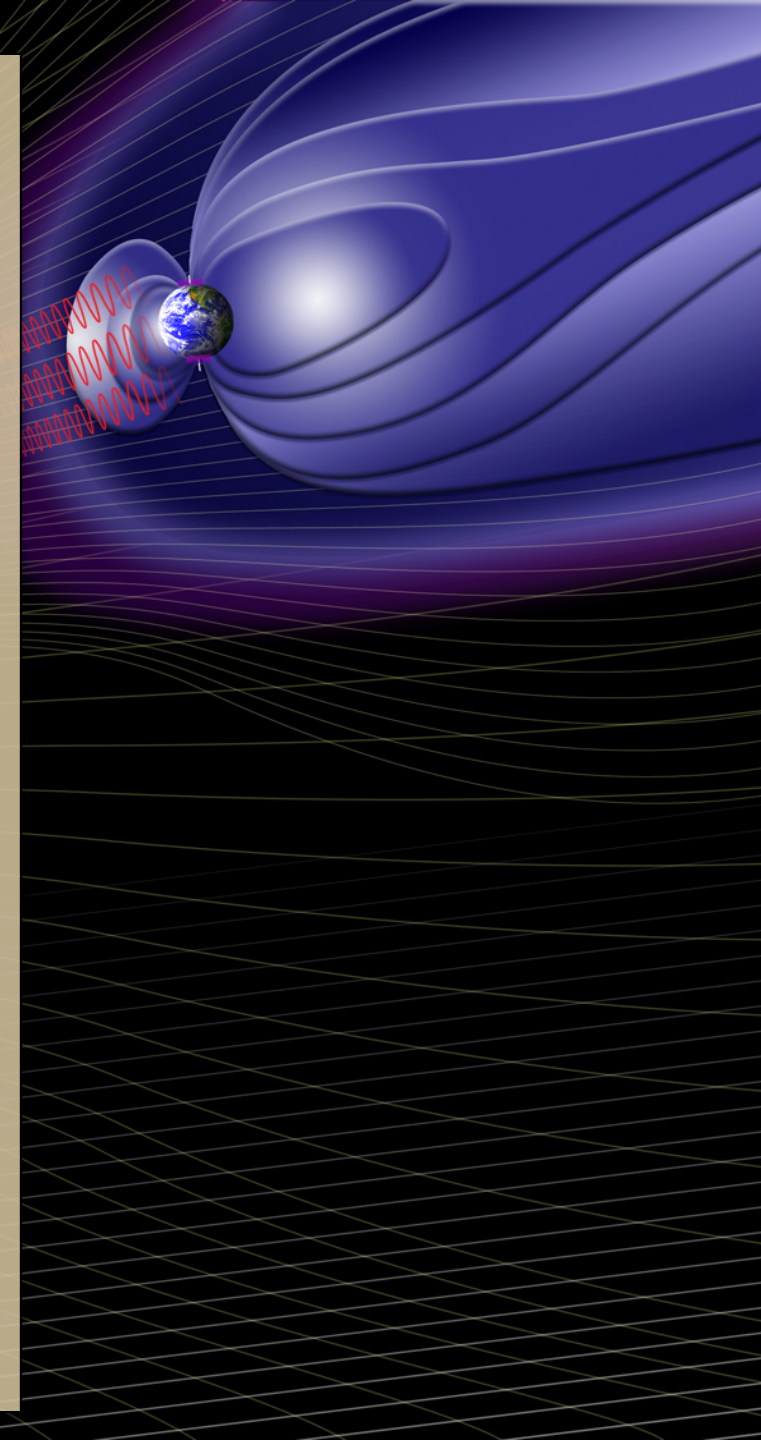
SPACE WEATHER CENTER

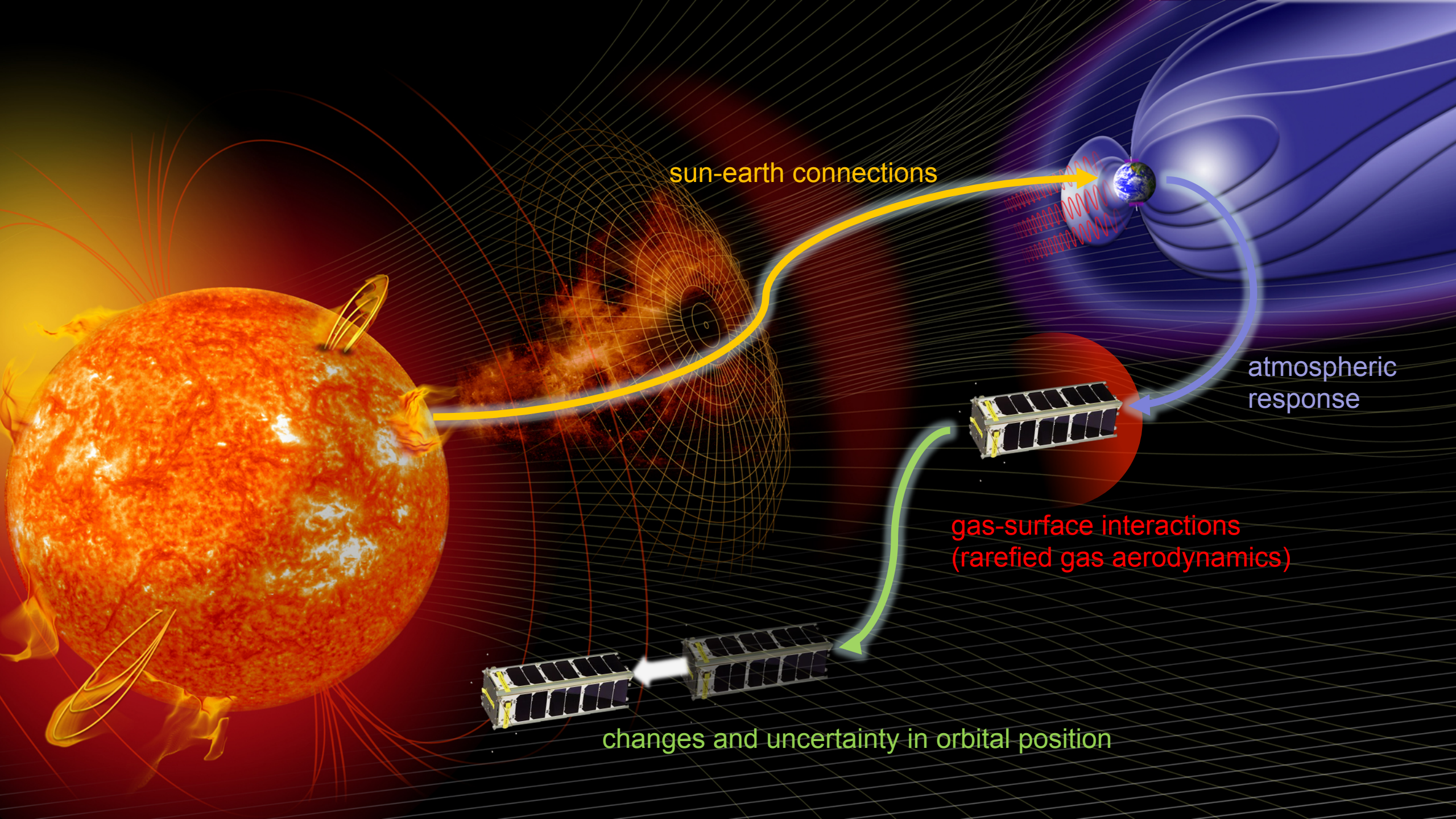


SWx-TREC

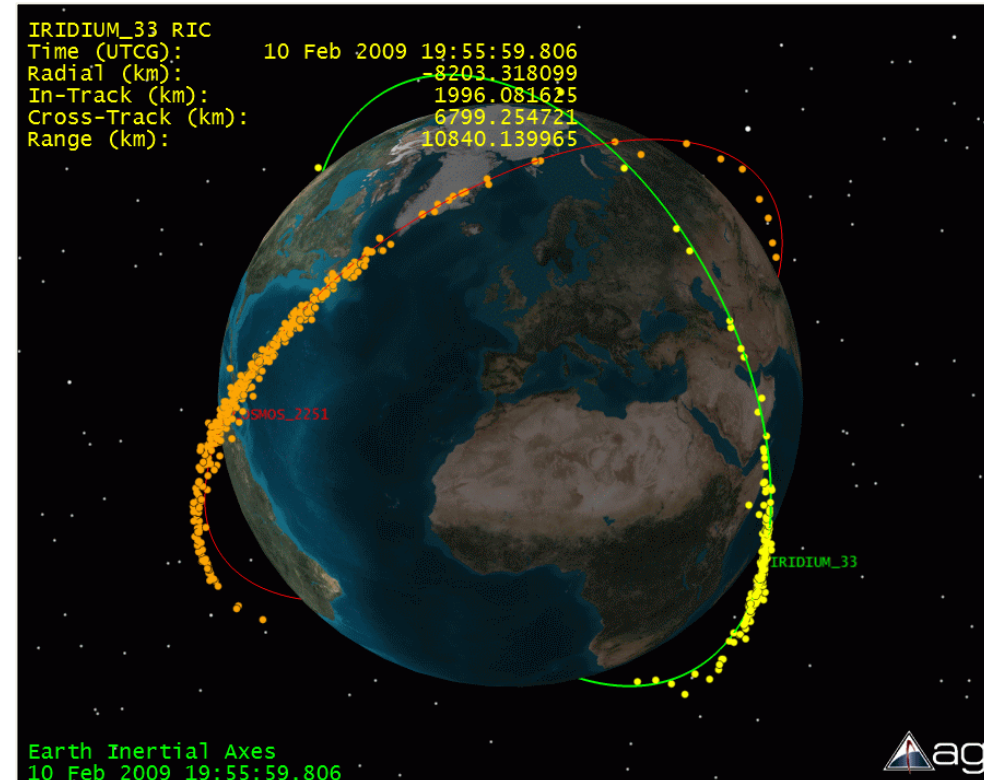
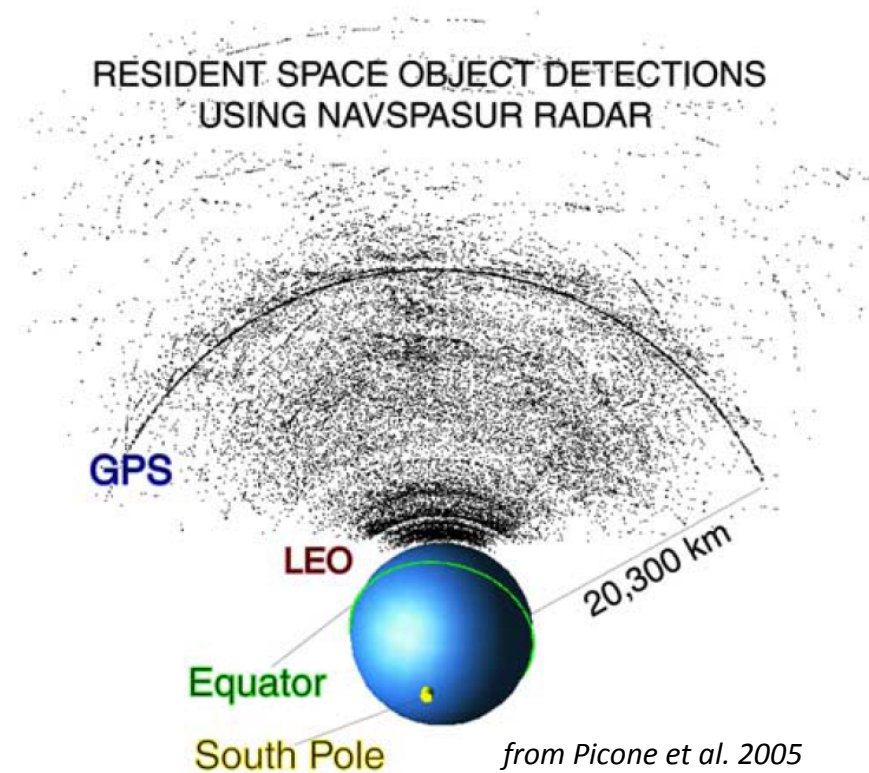
Satellite drag is one of our focus areas

- Interdisciplinary (Astrodynamics, Solar Physics, Aeronomy, Gas-Surface Physics, Modeling and Computation)
- "Problem of the Commons"
- Opportunities for O2R and R2O transitions





Resident Space Objects and the LEO Environment



Satellite drag errors degrade capability to: In 2016...

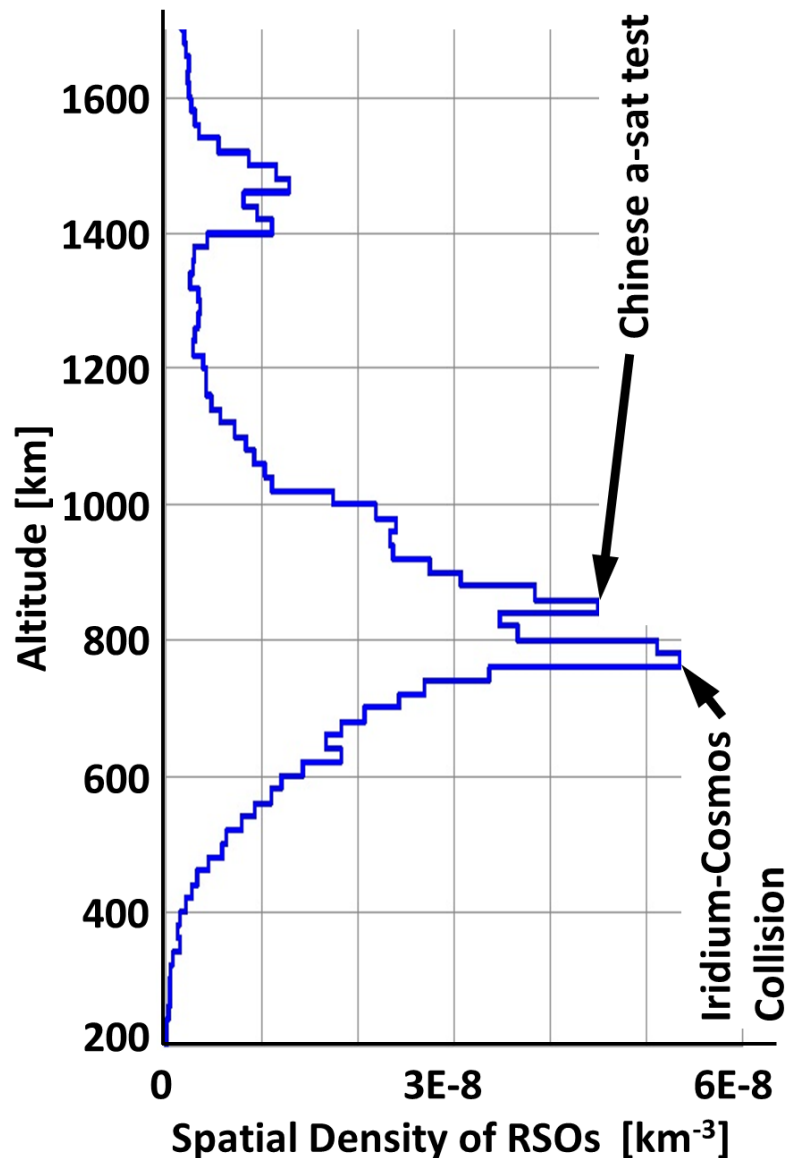
Total Number of CubeSats Launched
417

Total Number of Debris Generated by Cosmos-Iridium
1296

Total Number of Debris Generated by DMSP Satellites
346

Total Number of Debris Generated by Fengyun ASAT
3428

Resident Space Objects and the LEO Environment



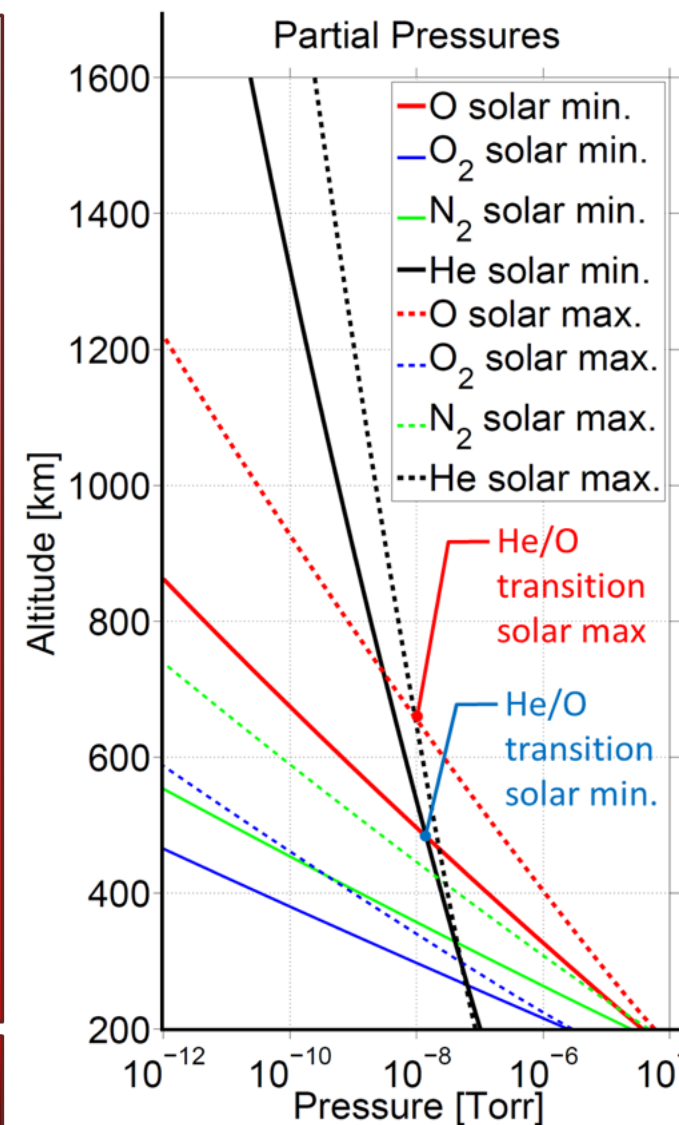
While SRP^1 is larger in magnitude, aerodynamic drag is the most variable force and the primary contribution to orbit errors

Drag is the dominant non-conservative force

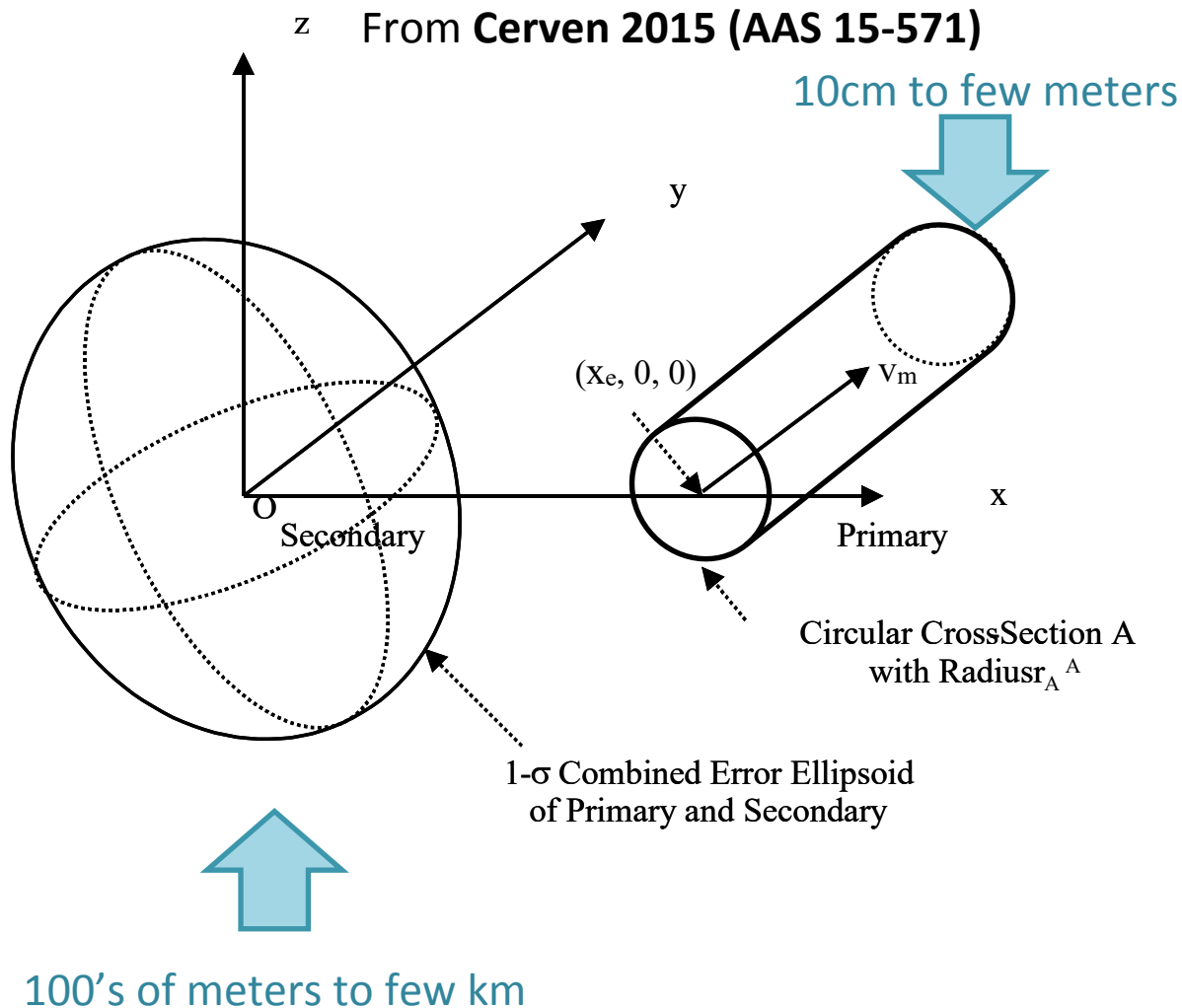
free-molecular flow

composition and temp. drives gradual changes in C_D

re-entry, extreme C_D variability



Predicting Collisions: Conjunction Analysis



- Collision Probabilities (P_c) determine the threshold for operational action
- General Assumptions
 - Two spheres
 - Gaussian probability distributions
- P_c is the “integral of the combined positional **error distribution** (C) within the tube swept out by the relative motion of the primary with respect to the secondary (v_m) given a combined hard body radius (r_a)” (Cerven 2015)

$$P_c = \iiint_V \frac{1}{\sqrt{(2\pi)^3 |C|}} e^{-\frac{1}{2} \mathbf{r}^T C^{-1} \mathbf{r}} dx dy dz$$

Conjunction Analysis

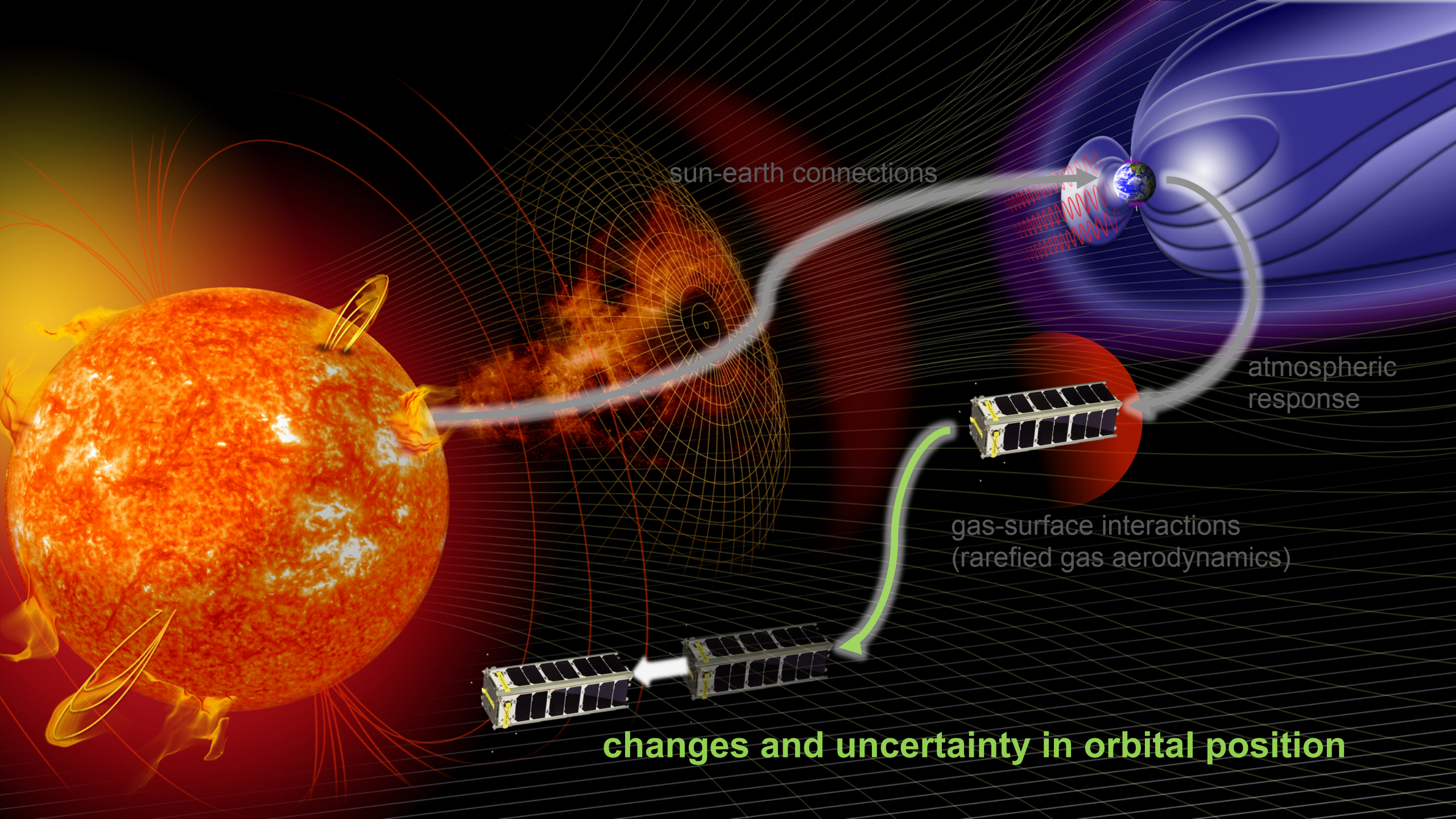


- Satellite Drag has a significant impact on P_c of LEO objects
 - Combined positional error distribution
 - Estimate of relative positions
- With the growing numbers of RSO's, number of warnings based on P_c is starting to be “not actionable”
 - over 18,000 conjunctions within 5 km for the coming 7 days
 - ~800 per day for NASA satellites alone

Other Satellite Drag Impacts

- Re-Entry Predictions
 - Involves lower atmosphere dynamics
 - Flight dynamics in the lower Thermosphere and Mesosphere
 - Transition from free molecular flow to rarefied gas dynamics
- Mission Lifetime Estimates
 - Long term estimates of solar activity and atmospheric response





sun-earth connections

atmospheric
response

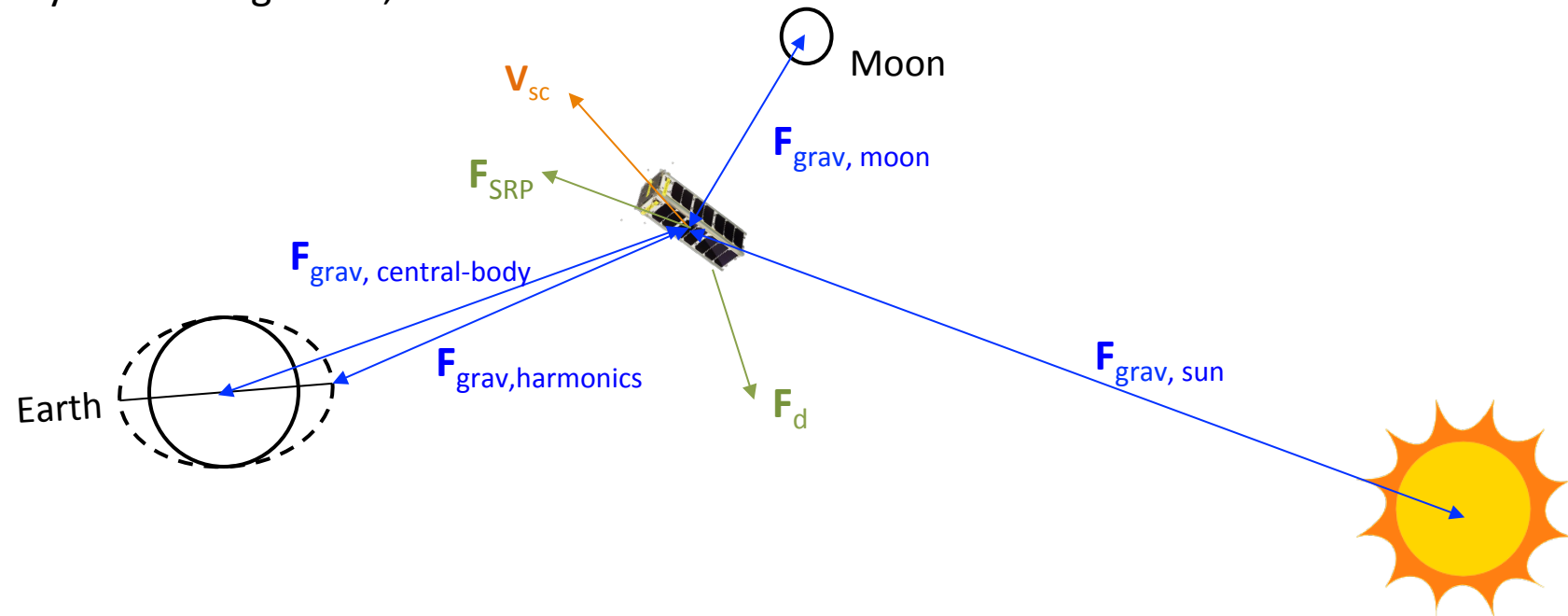
gas-surface interactions
(rarefied gas aerodynamics)

changes and uncertainty in orbital position

Orbital Perturbations



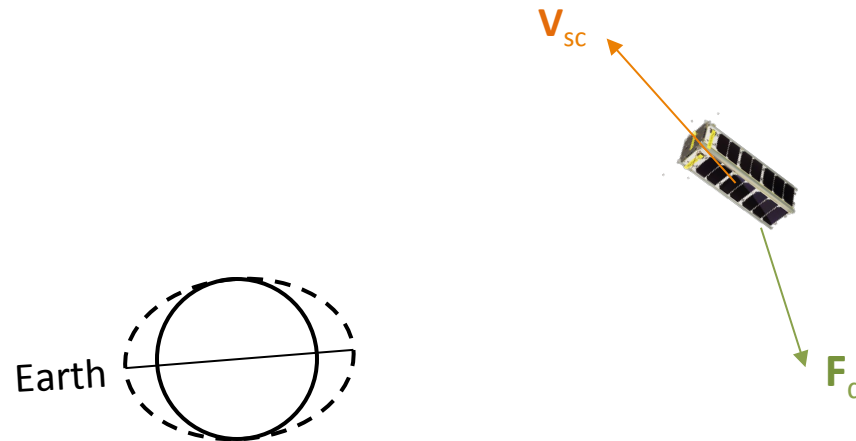
- V_{sc} Spacecraft Velocity
- F_{grav} Gravitational Forces
- F_{SRP} Solar Radiation Pressure, Surface Force
- F_d Aerodynamic Drag Force, Surface Force



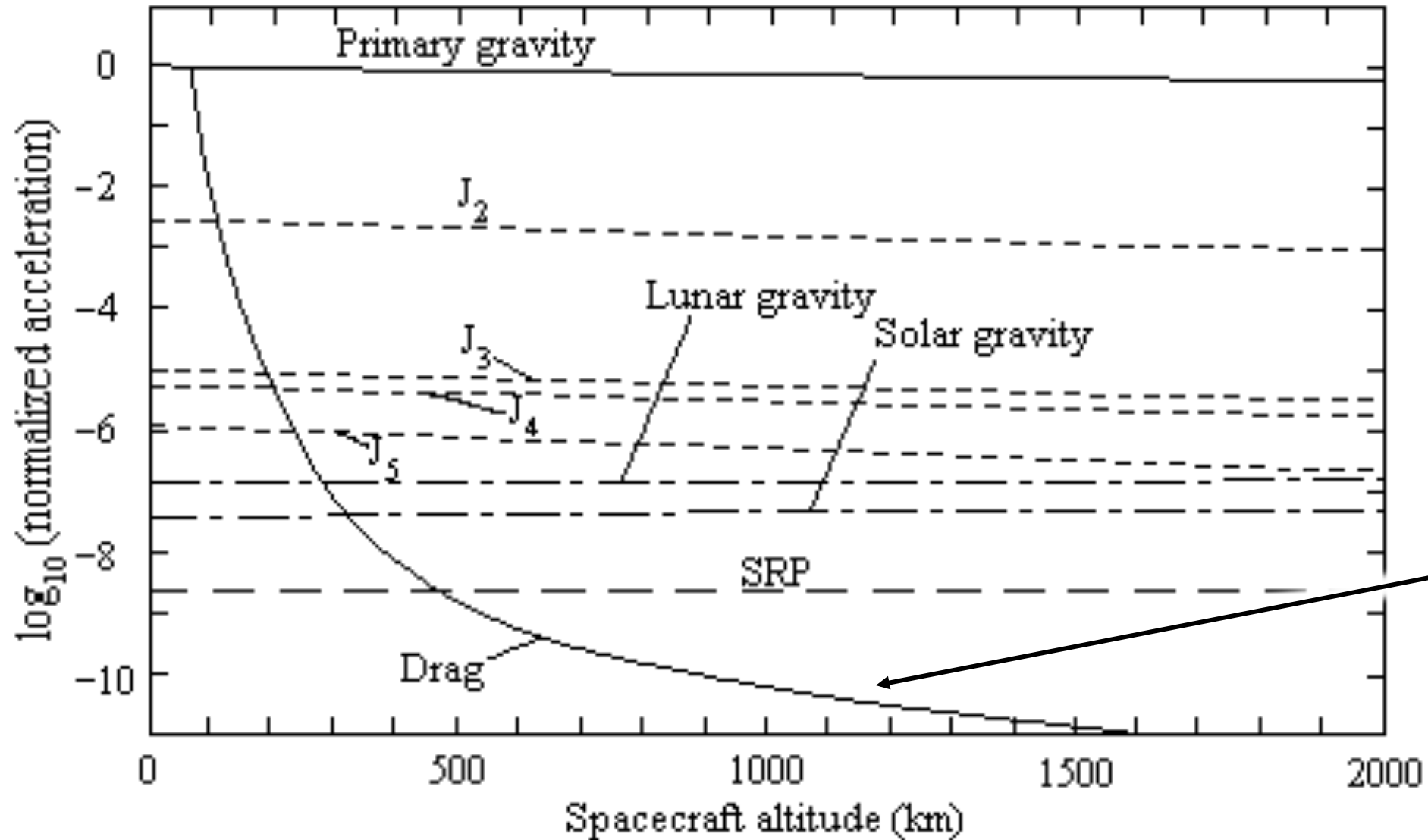
Surface Forces



- V_{sc} Spacecraft Velocity
- F_{grav} Gravitational Forces
- F_{SRP} Solar Radiation Pressure, Surface Force
- F_d Aerodynamic Drag Force, Surface Force



Orbital Perturbations

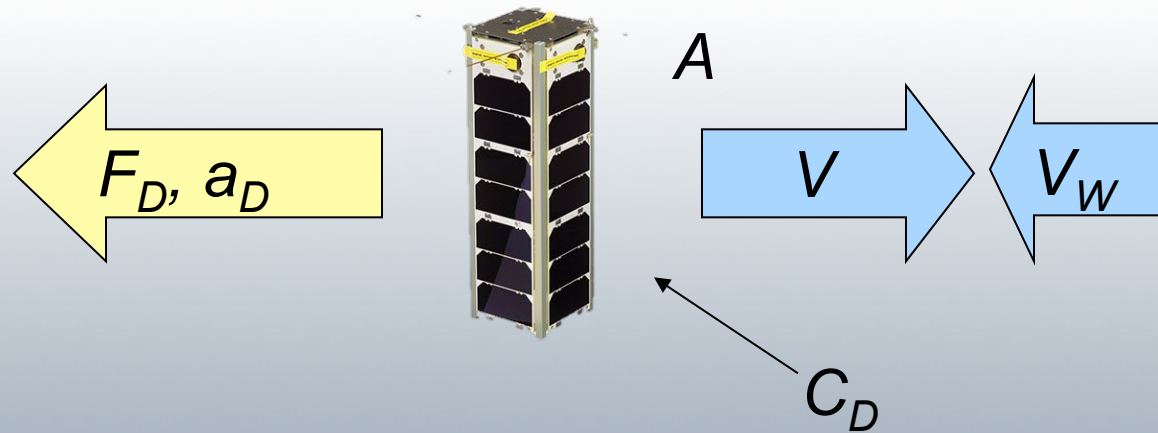


Most variable and uncertain of any of the other perturbations

Astrodynamics of Satellite Drag



$$\mathbf{a}_D = -\frac{1}{2} \rho \frac{C_D A}{m} V_{rel}^2 \hat{\mathbf{V}}_{rel}$$



atmosphere

ρ – *density*

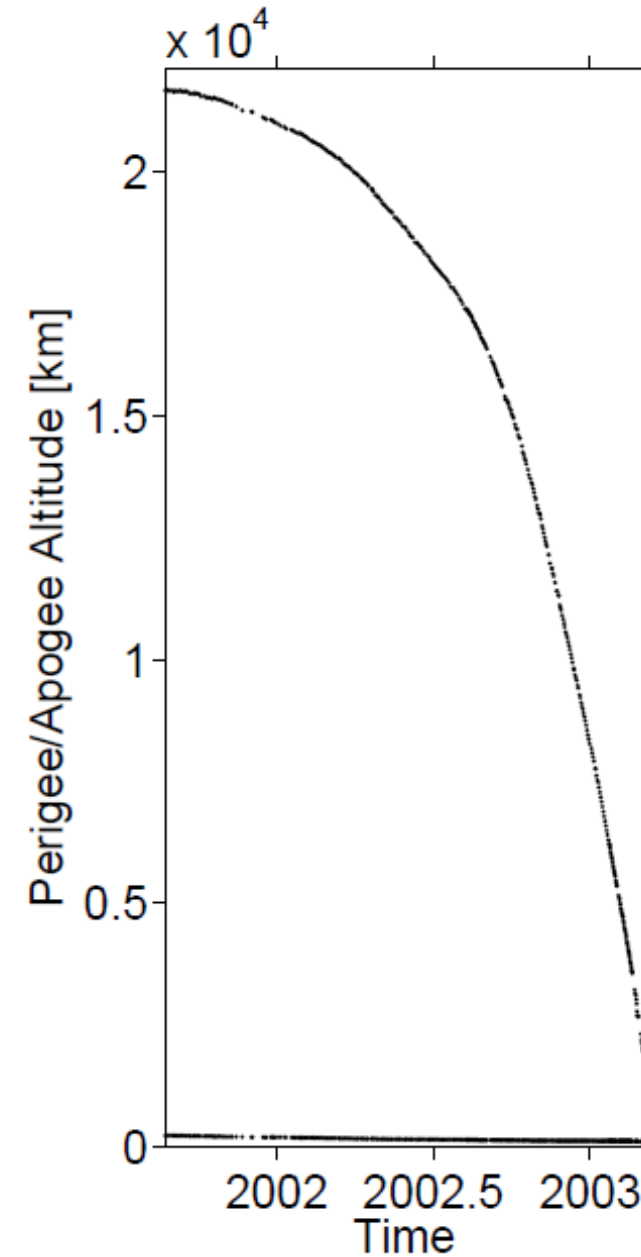
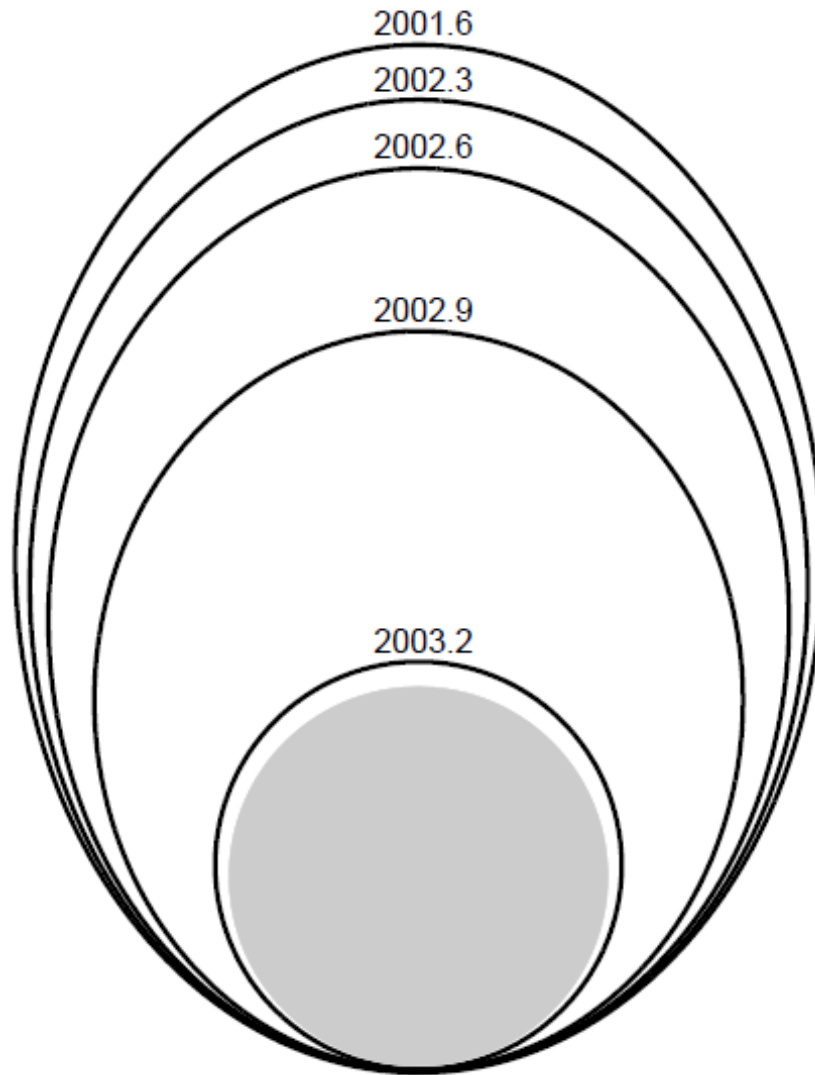
T_a –
temperature

composition

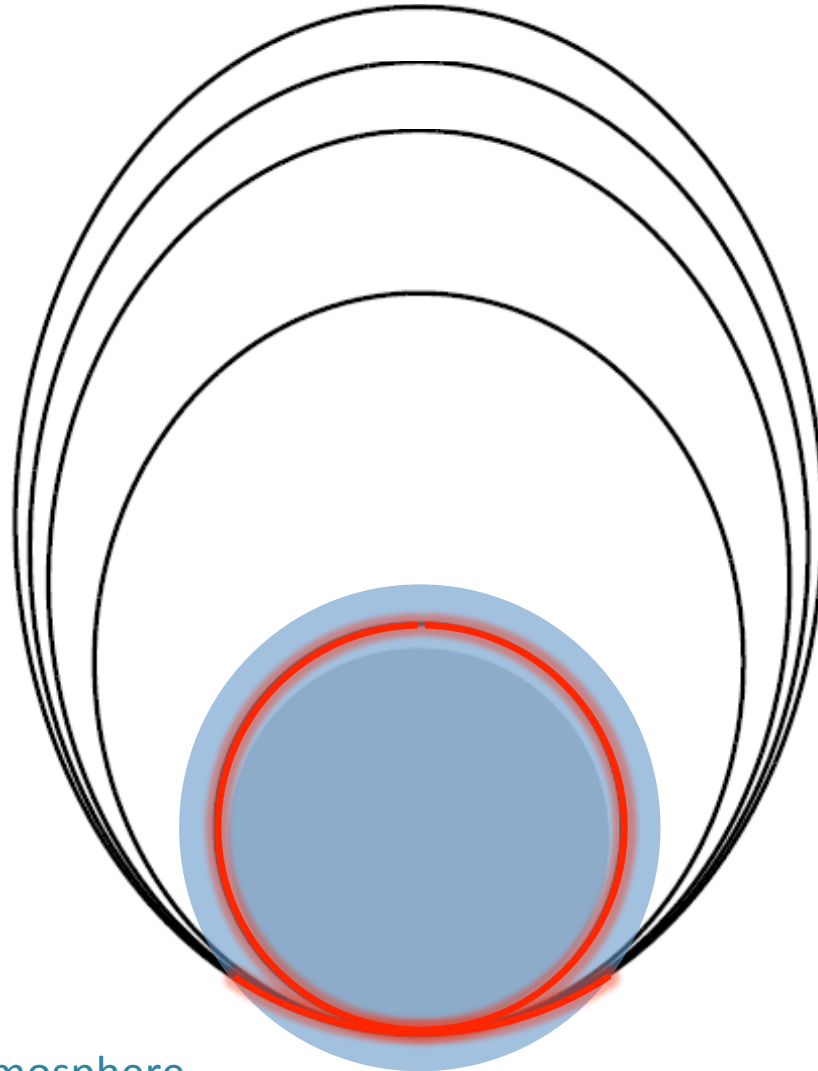
F_D drag force
 A cross sectional area
 C_D drag coefficient
 V spacecraft velocity
 V_w atmospheric winds

\mathbf{V}_{rel} vector sum of \mathbf{V} and \mathbf{V}_w

An Illustration of Orbital Decay



Energy Dissipation Rate (EDR)



atmosphere

orbital energy dissipation

Work done by aerodynamic drag along the orbital path l

$$B/2 \rho \|V\| r \| \dot{r} \| l$$

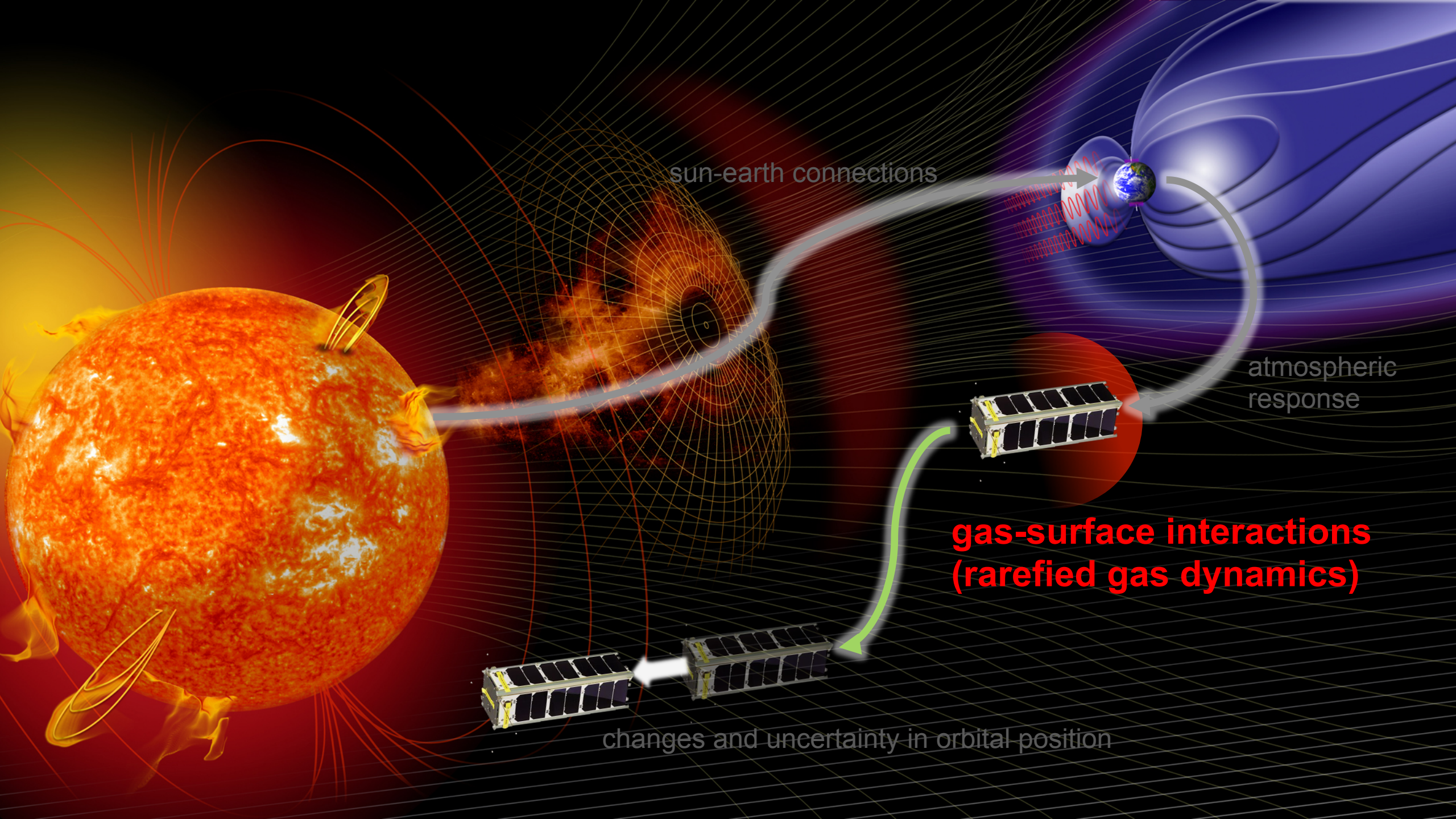
Rewriting as a line integral, separating the "constant" terms, and dividing by a time interval results in the EDR

$$\varepsilon = 1/2 \Delta t \int_{t_i}^{t_k} B \rho \|V\| r \| \dot{r} \cdot V \|_{sat} dt$$

Assuming there are no significant in-track SRP effect nor 3rd body effects or that these can be removed, we can relate the EDR to change in mean-mean motion

$$\dot{\varepsilon}_{\text{obs}}(t_{ik}) = \frac{\Delta n}{3n_A \mu^{-2/3} \Delta t}$$

Mean motion, n , determines where the satellite will be along its orbit at any given time (in track motion)



sun-earth connections

atmospheric
response

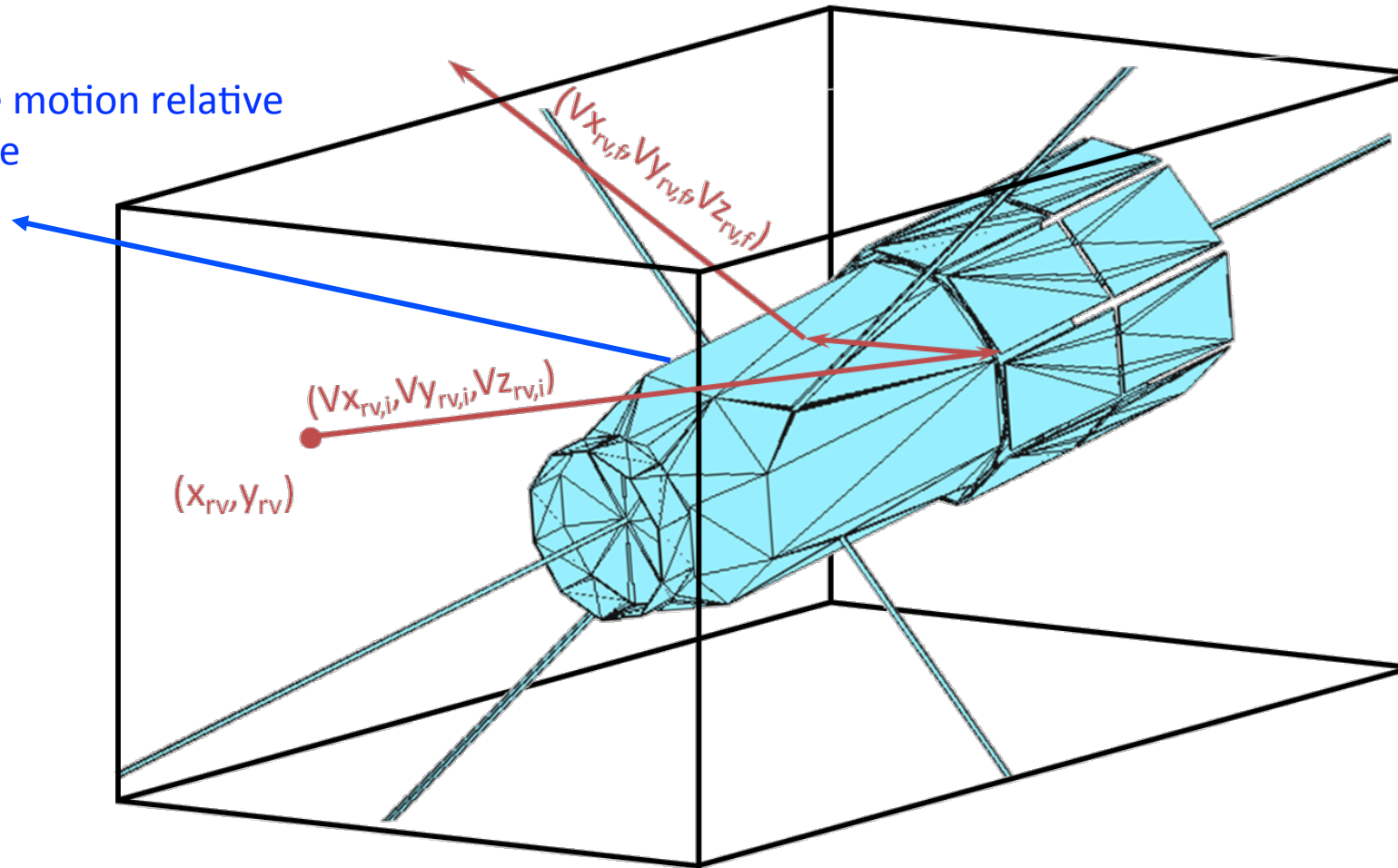
**gas-surface interactions
(rarefied gas dynamics)**

changes and uncertainty in orbital position

Computing Aerodynamic Forces

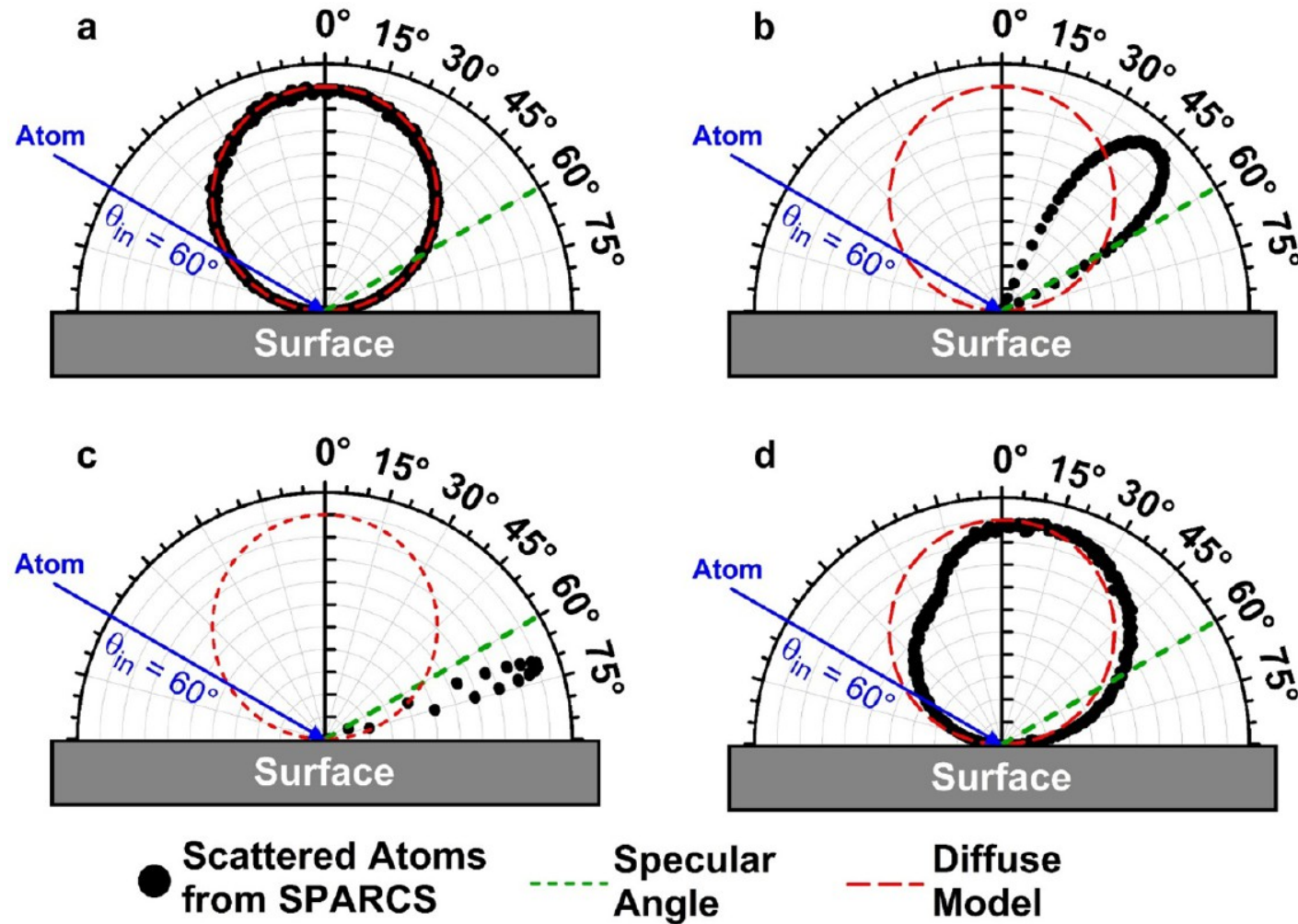


Direction of satellite motion relative
to the Thermosphere



- Aerodynamics force is the sum of total molecular momentum change over a certain time
- Hotter flow can reach the side and back areas of satellites (the Thermosphere is hot)

Gas-Surface Interactions

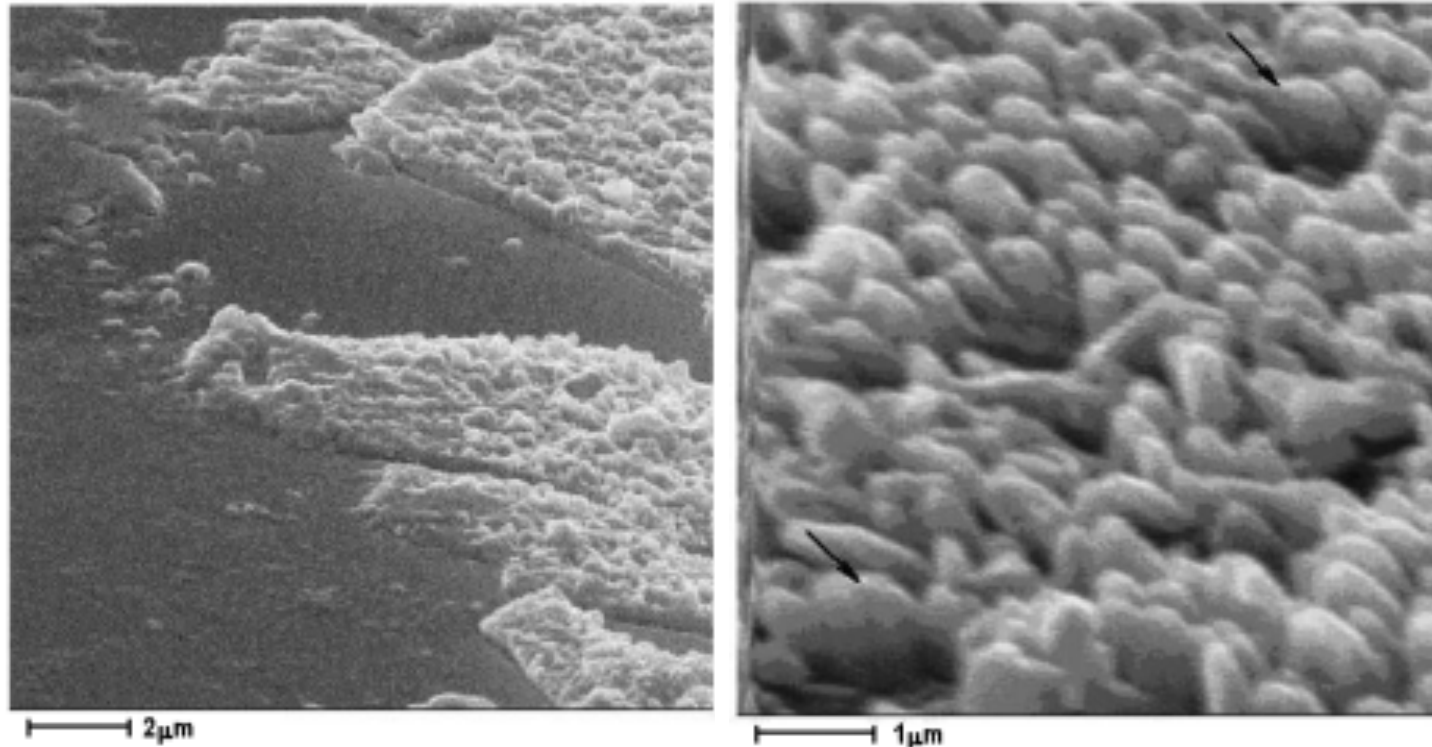


From Murray et al. 2017

Gas-Surface Interactions

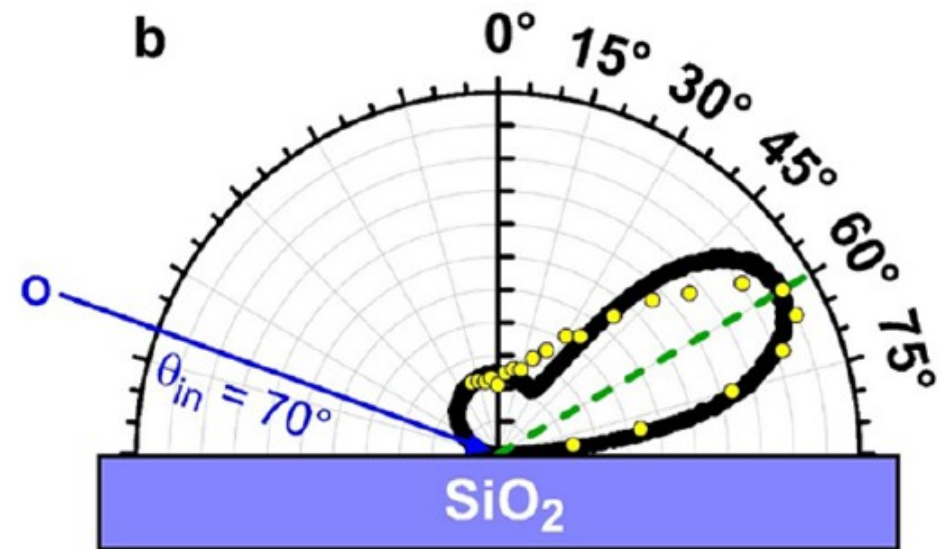
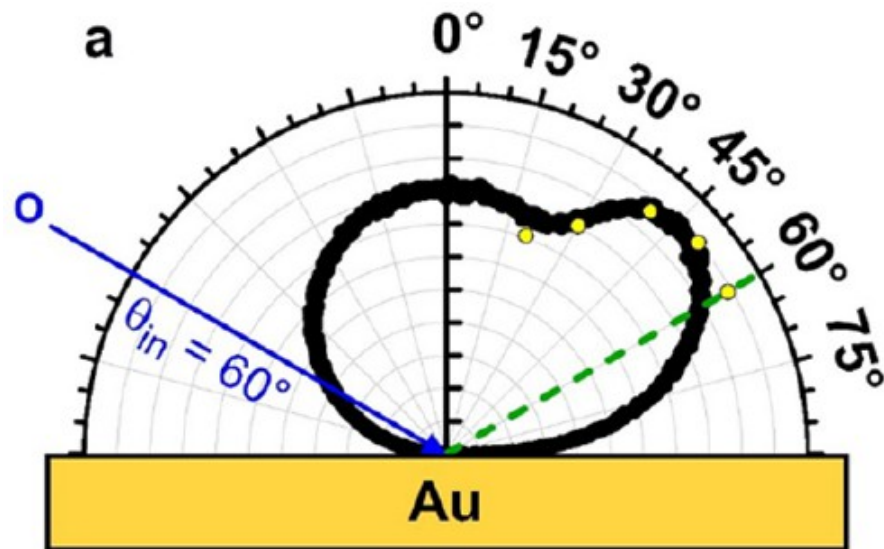


Skurat et al. 2011 (Journal of Spacecraft and Rockets)

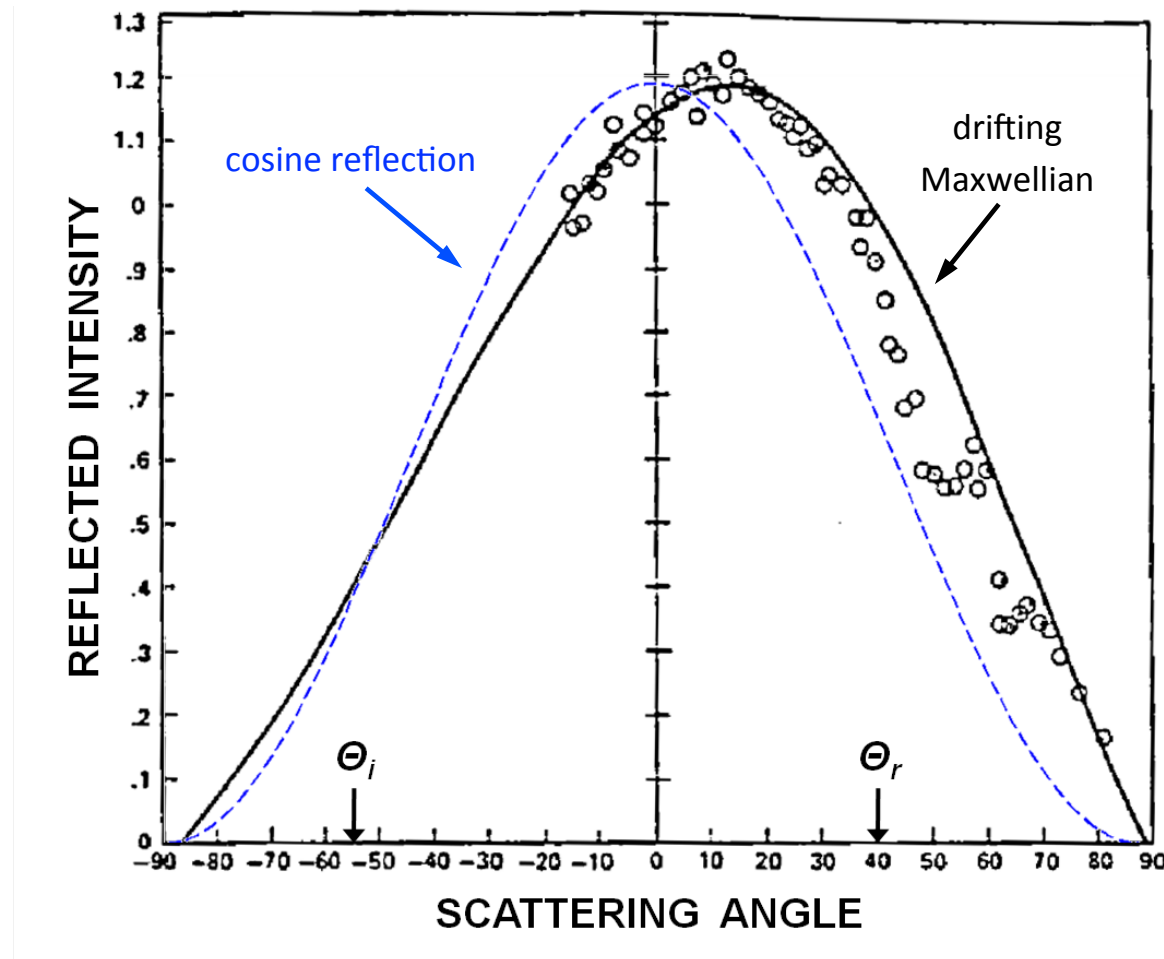


*diameter of a strand of hair is $\sim 100 \mu\text{m}$,
length of N_2 molecule is $\sim 0.0003 \mu\text{m}$*

Laboratory Experiments



Experience from Spacecraft Observations

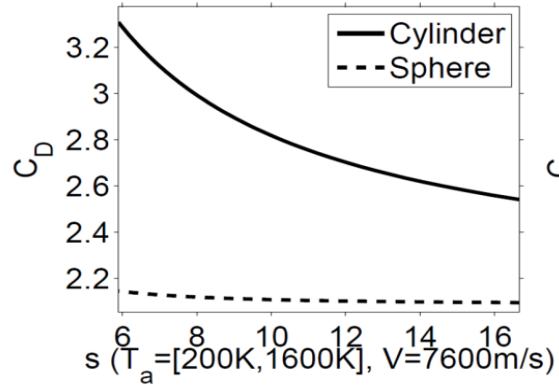


- Gregory and Peters found 98% reflect diffusely at shuttle altitudes and incident flow was completely accommodated [Gregory and Peters 1987]

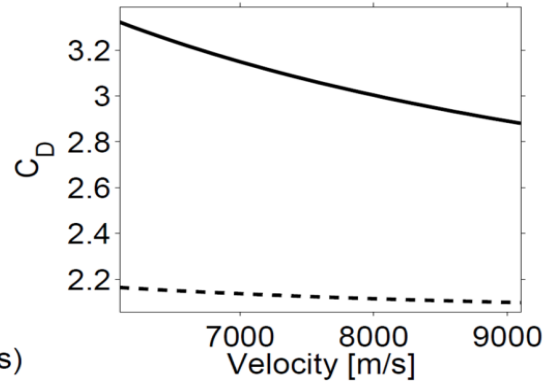
Drag Coefficient Sensitivities



Thermal to bulk
velocity ratio



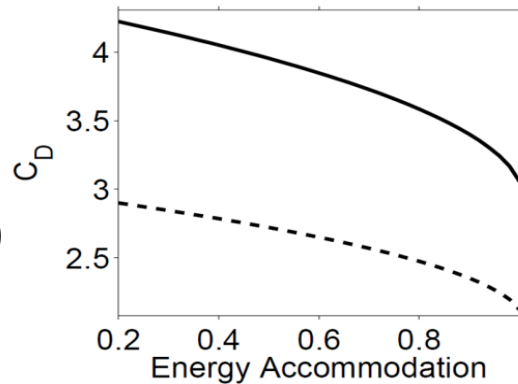
Spacecraft
velocity



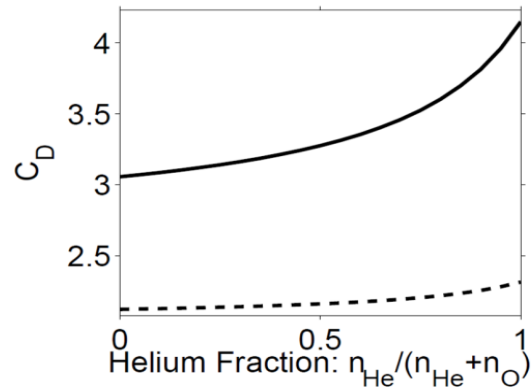
Cylinder of length to diameter
ratio of 3 unless otherwise stated



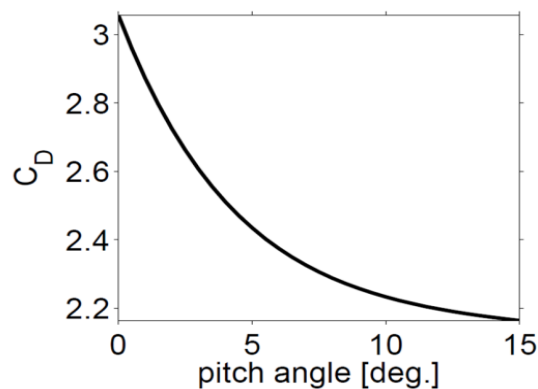
Energy exchange
with surface
(Energy-
Accommodation)



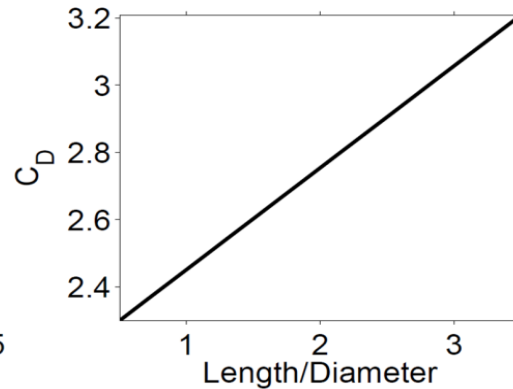
Composition



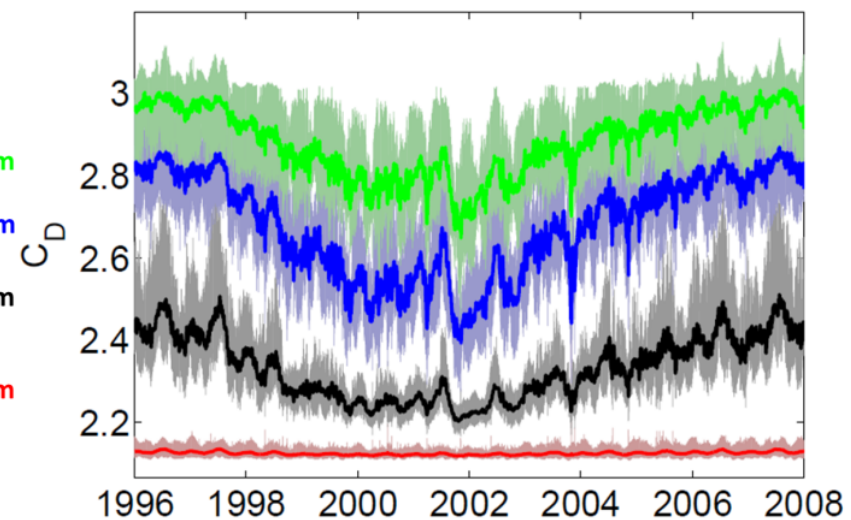
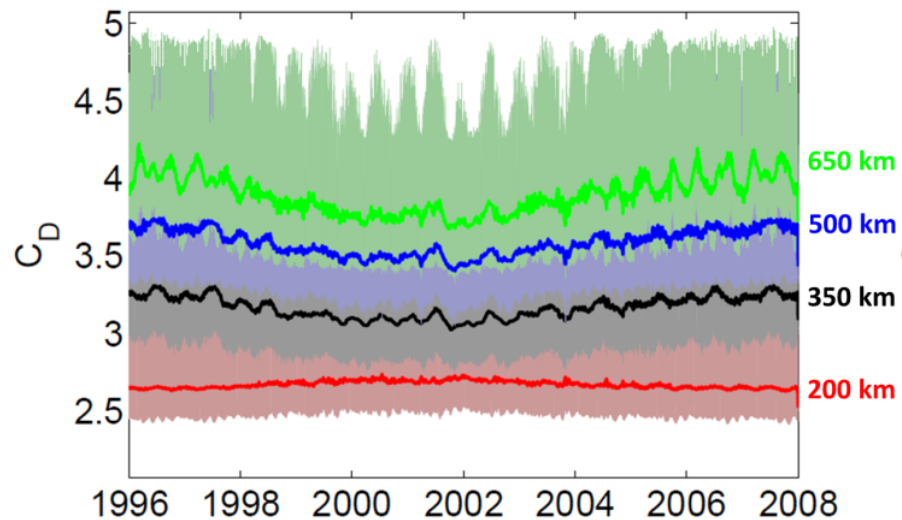
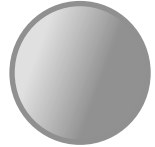
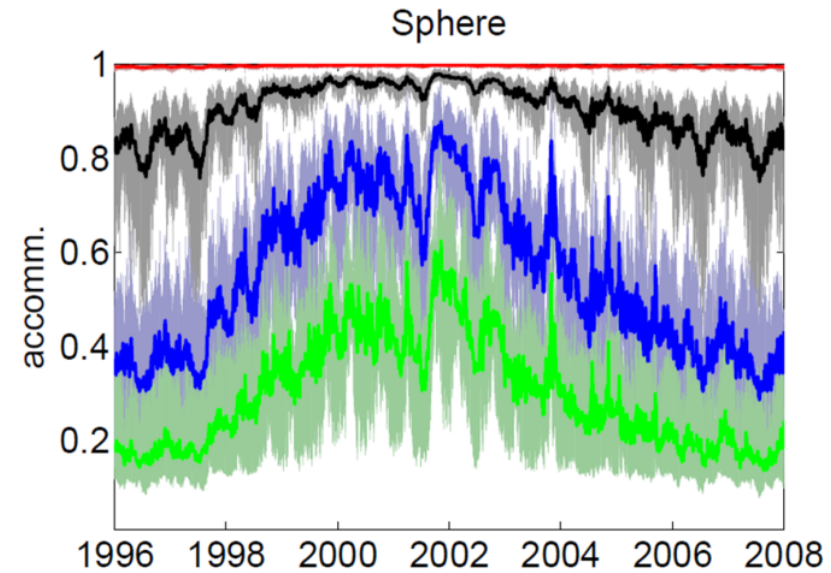
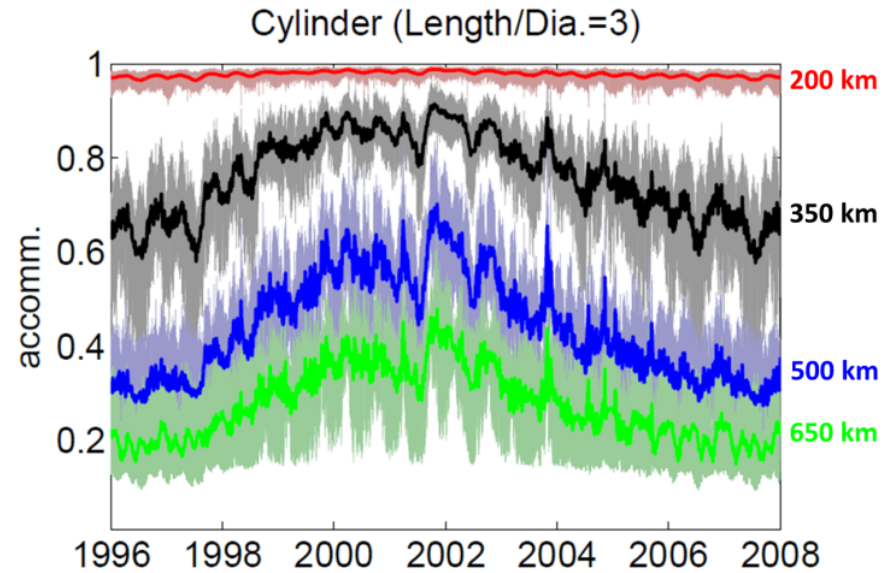
Attitude



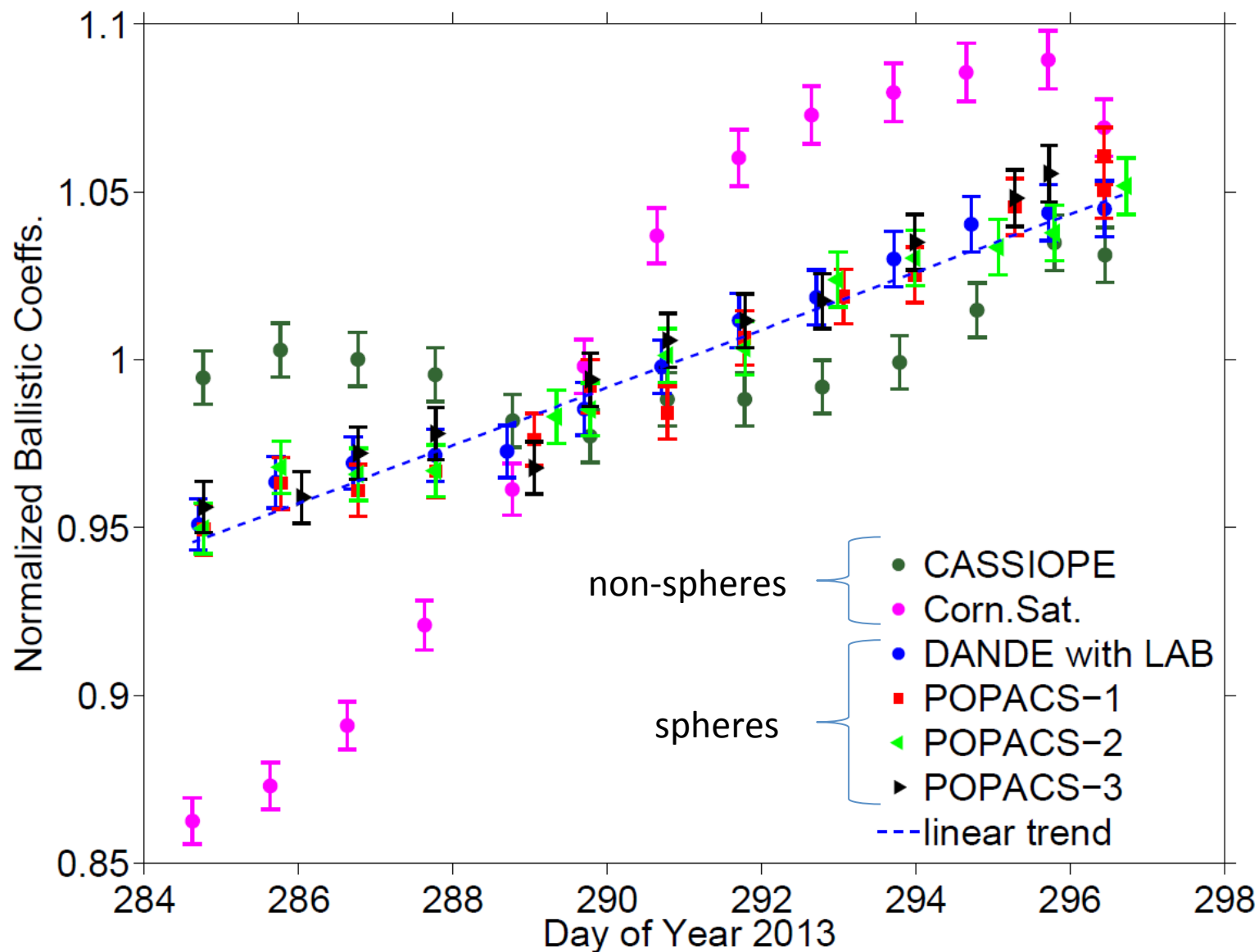
Shape



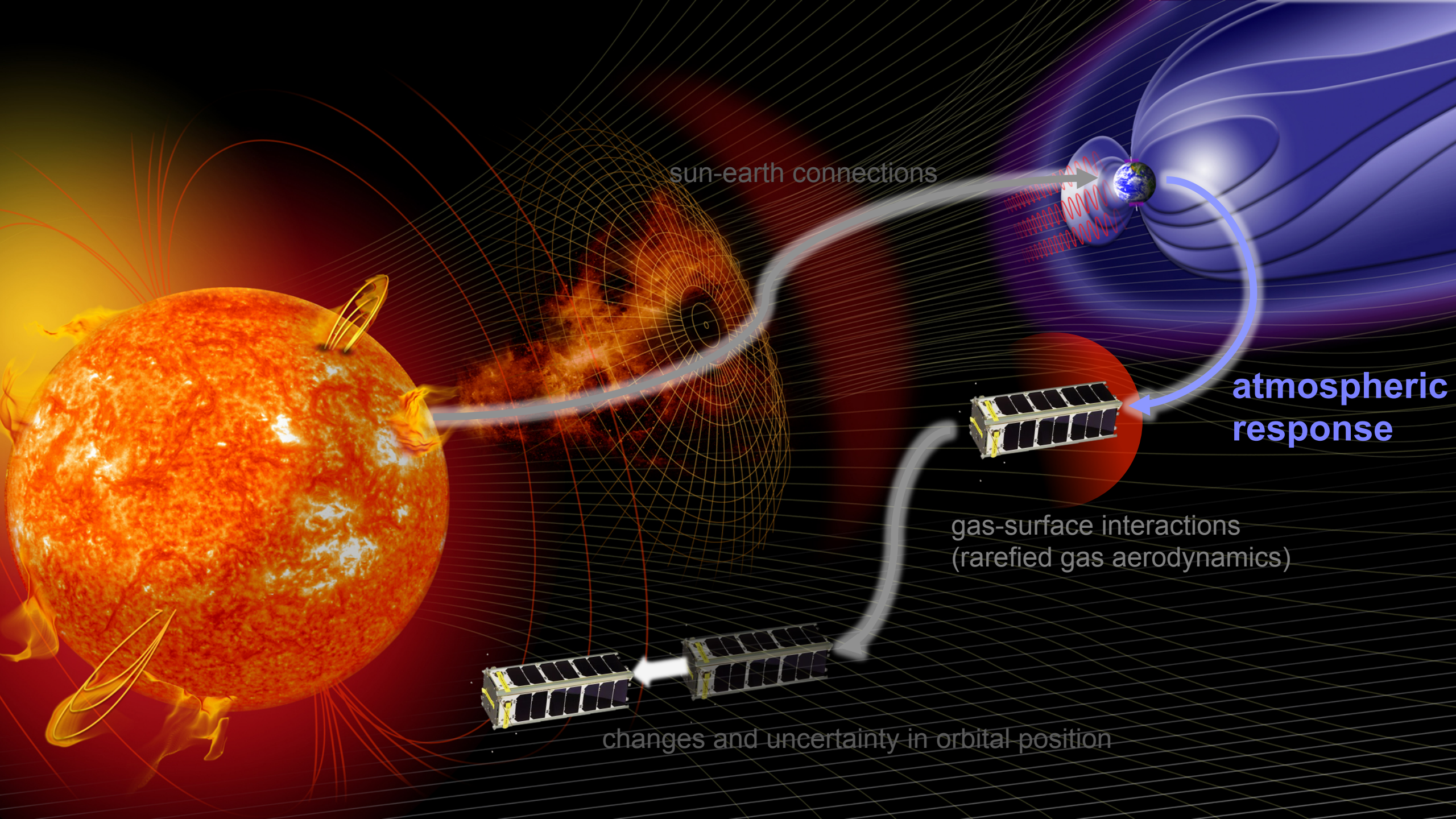
Drag Coefficient Sensitivities



Cross-Sectional Area Variability



- Six satellites flying in close formation
- Decrease in density with time causes a secular trend in the fitted ballistic coefficient
- Spherical objects cluster around the secular trend
- Non-spherical objects change their cross sectional areas and exhibit significant ballistic variability



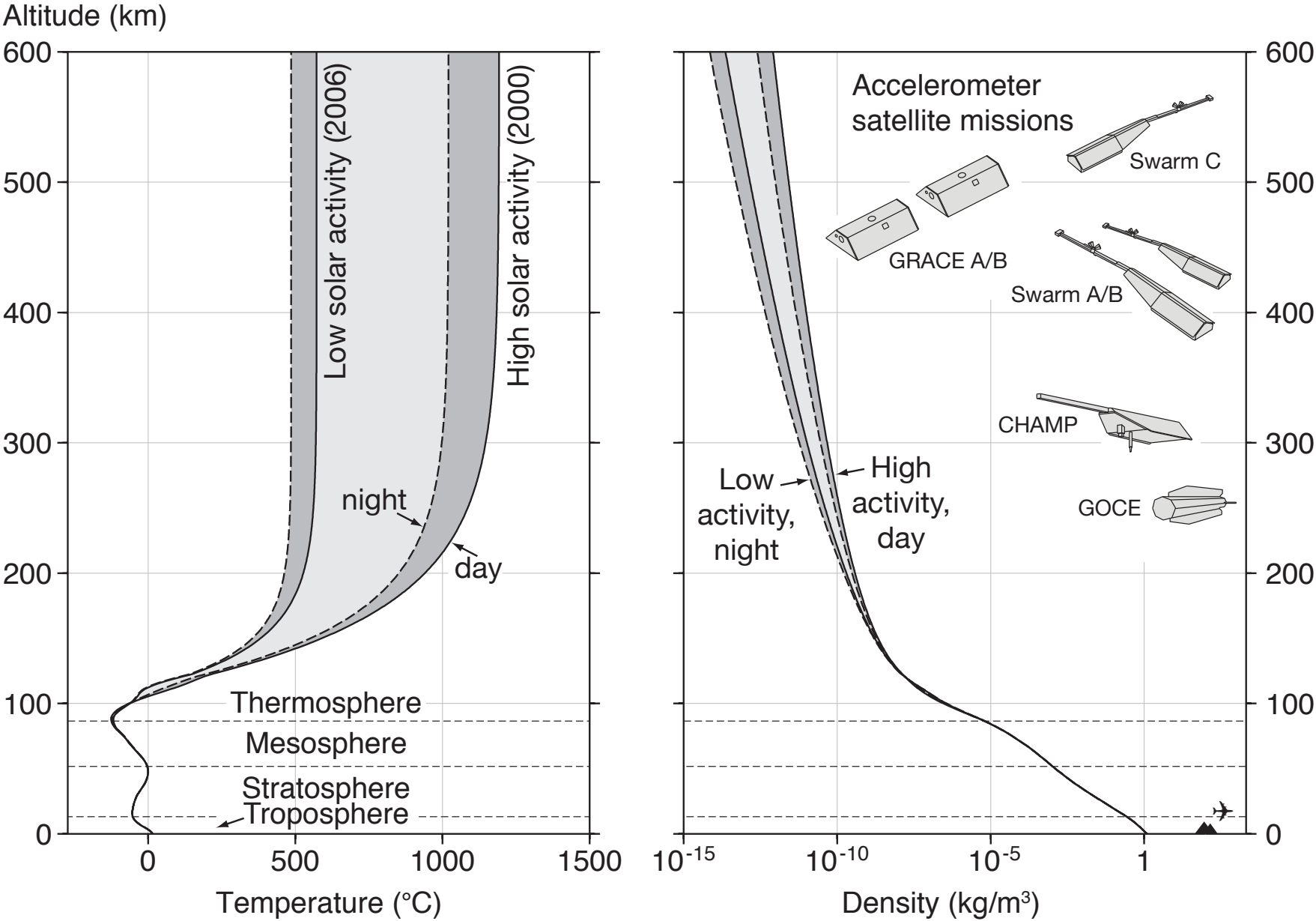
sun-earth connections

atmospheric
response

gas-surface interactions
(rarefied gas aerodynamics)

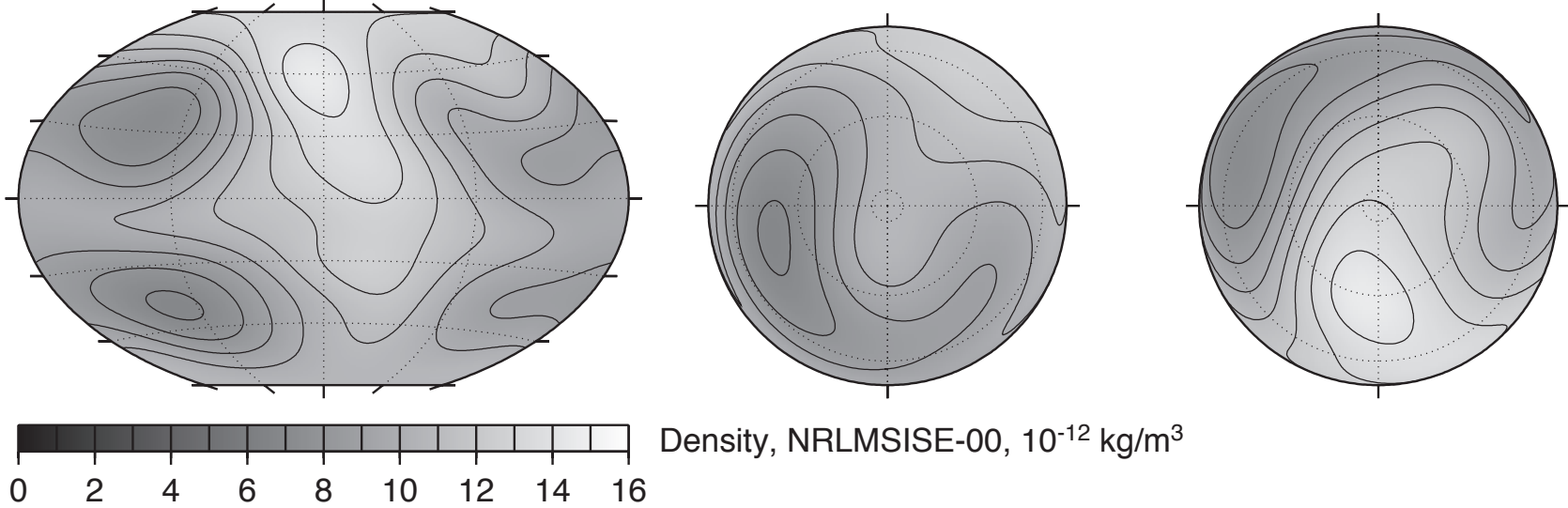
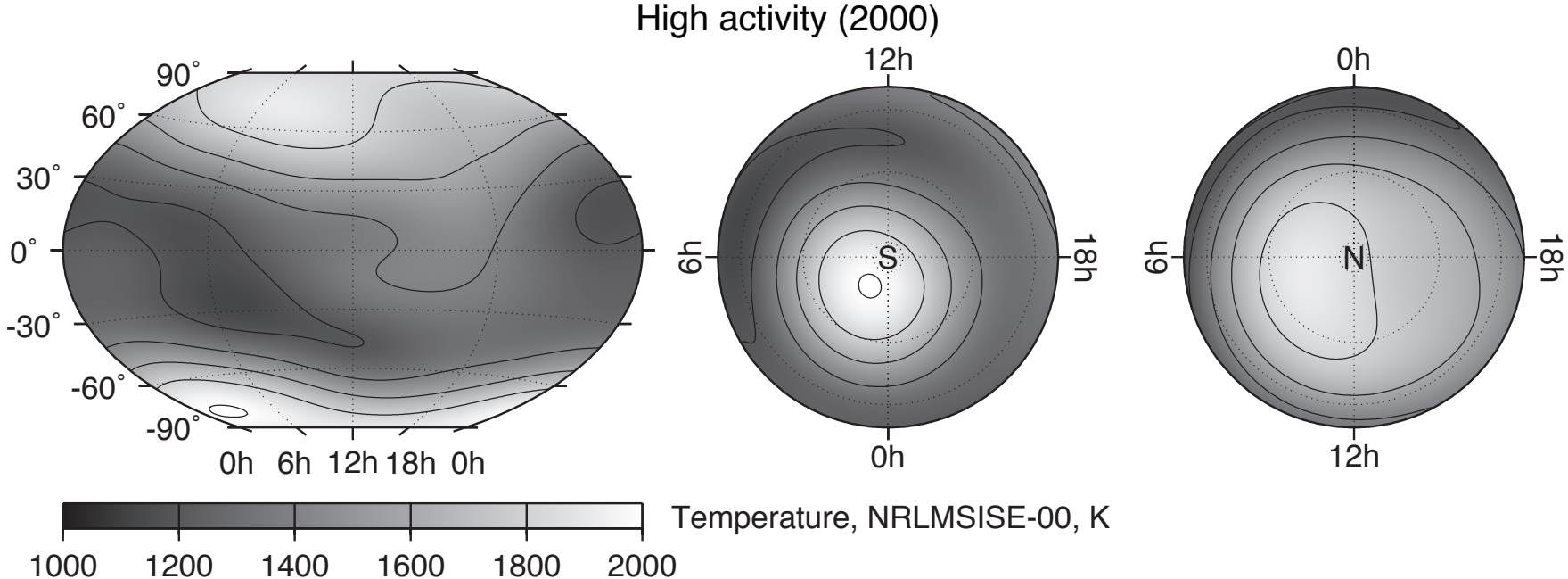
changes and uncertainty in orbital position

Atmospheric Densities



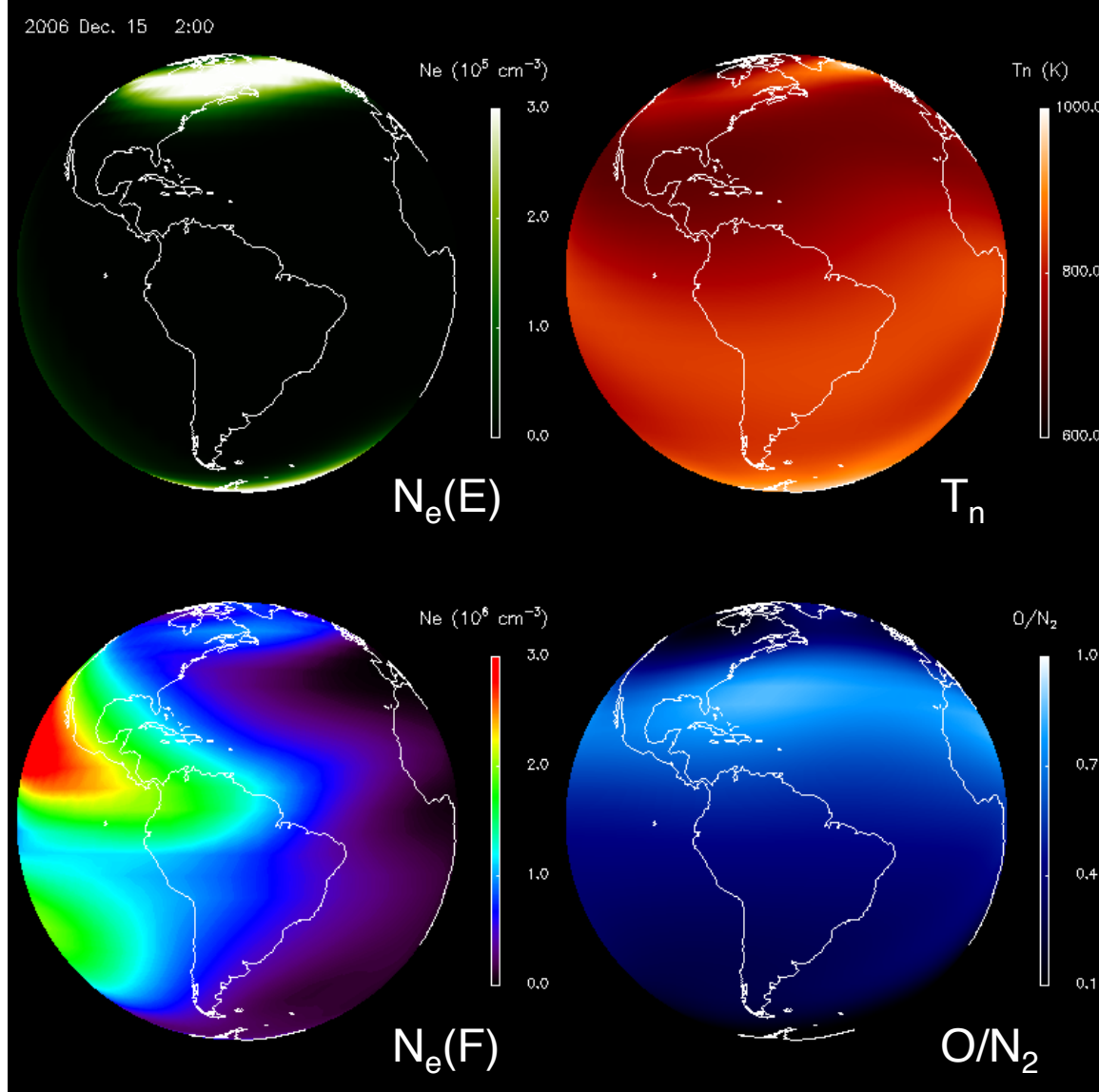
From Doornbos
2011

Atmospheric Densities (from and empirical model)



From Doornbos
2011

Global Circulation Models: Example



- Coupled momentum and continuity equations
- Runs-on-request at CCMC
- More information at:
<http://www.hao.ucar.edu/modeling/tgcm>
- Other GCM's include
 - GITM
 - TIME-GCM
 - CTIPe
 - WAM
 - WACCM
 - ...

Thermospheric Data Assimilation

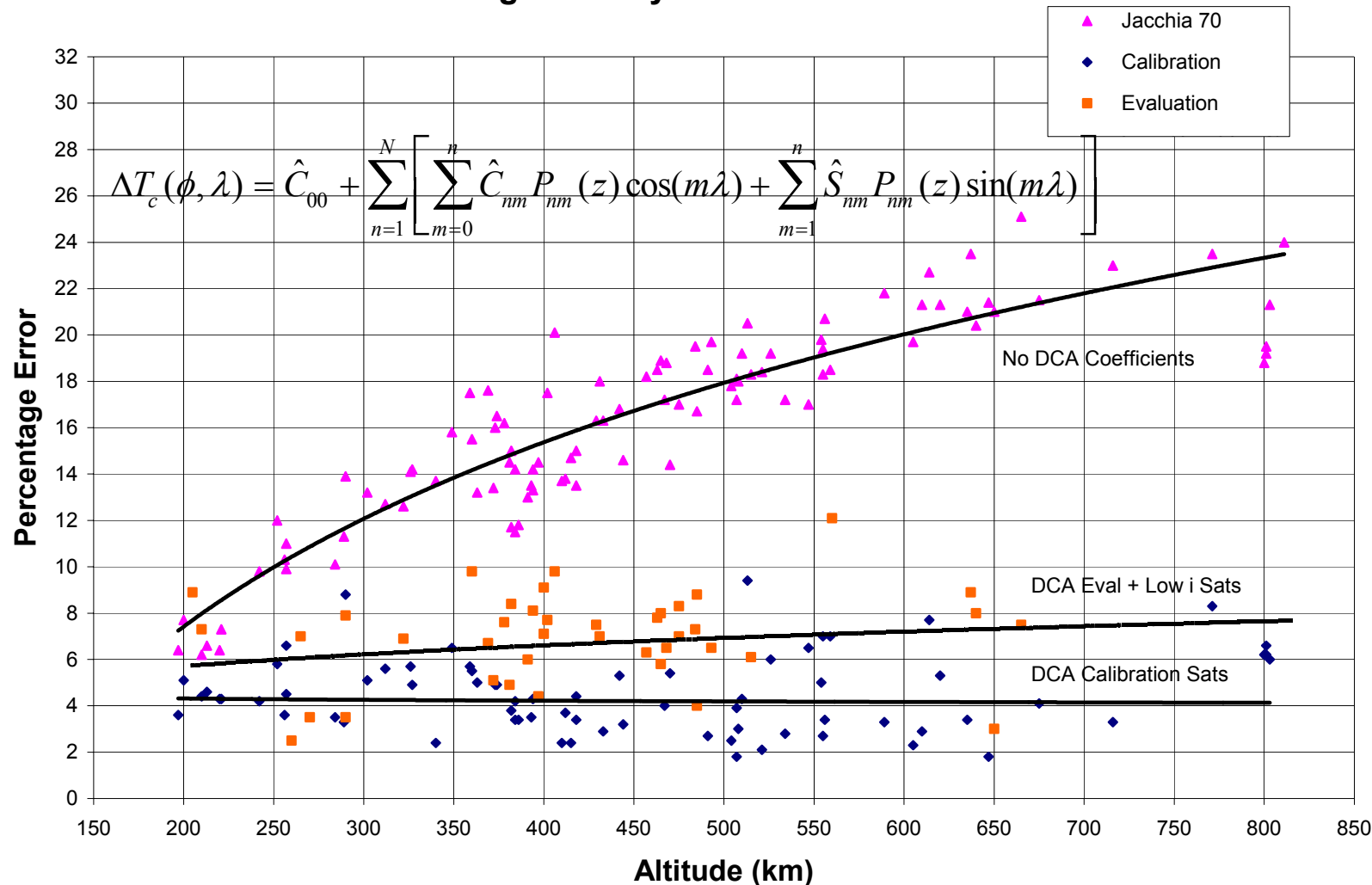


Combining data and thermospheric models, and satellite aerodynamics we can constrain the satellite drag problem

High Accuracy Satellite Drag Model (HASDM)



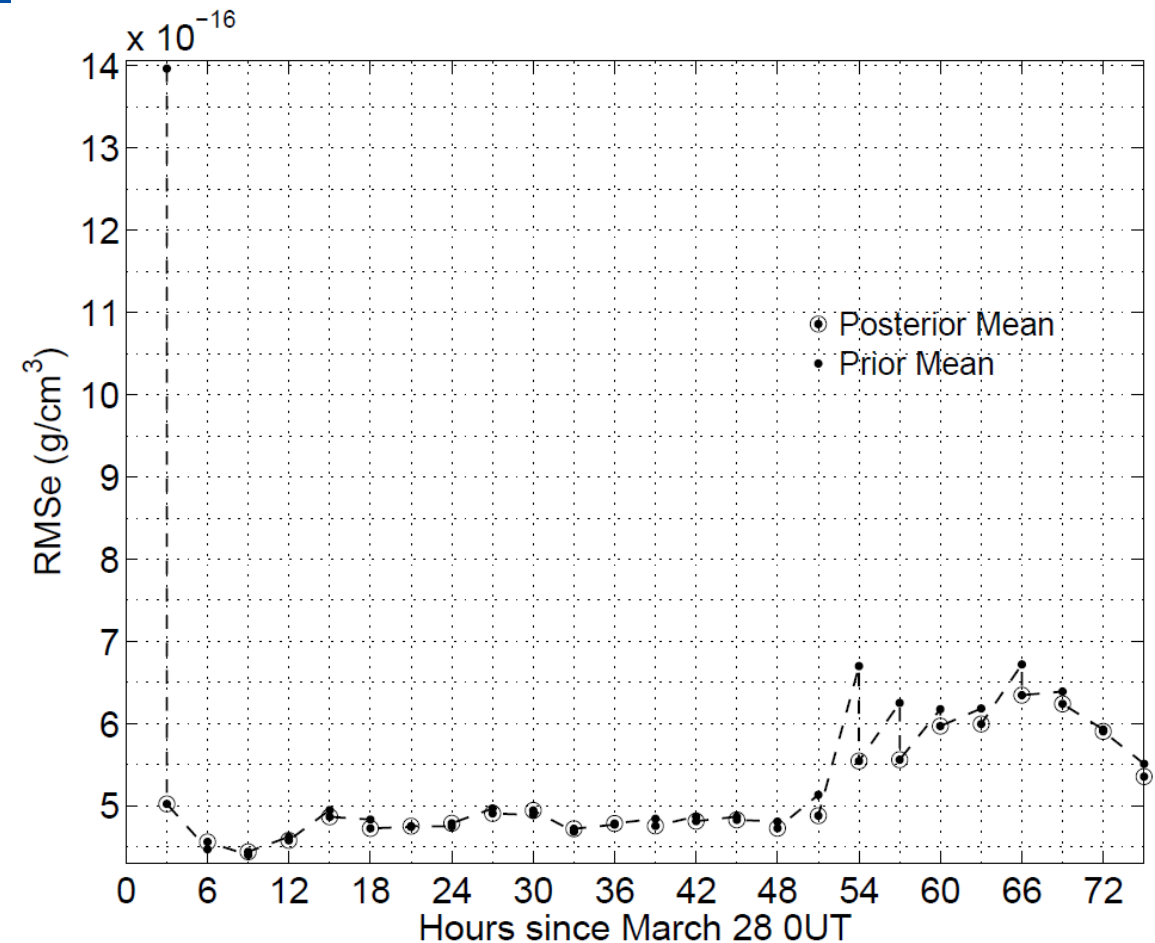
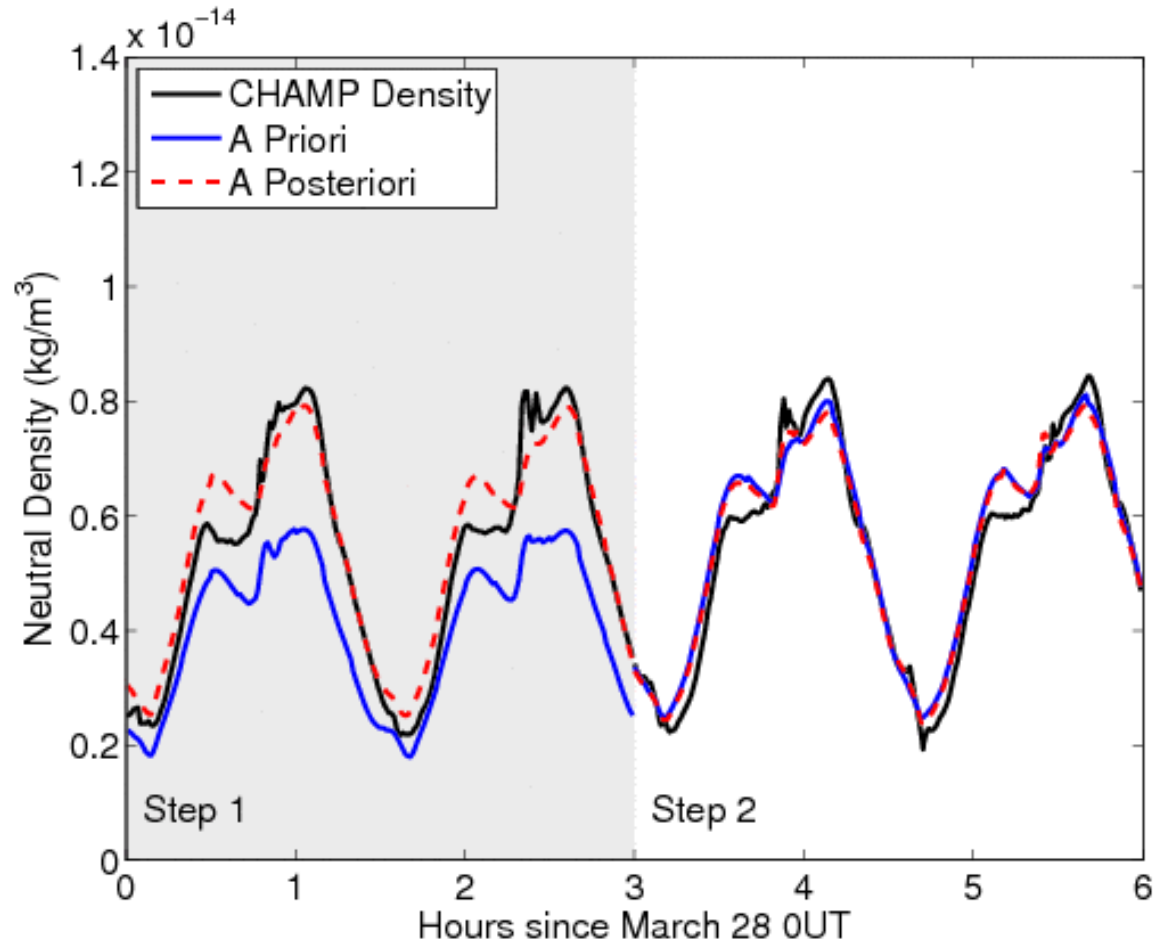
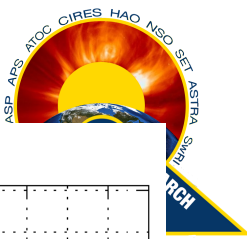
Average Density Error versus Altitude



- Atmospheric temperatures in a 4x4 spherical harmonic expansion at two altitudes are included in the orbital fitting process for a set of ~70 calibration satellites
- Uses orbit or daily average satellite tracking data from AF radars
- Jacchia-type empirical model used as background for the assimilation

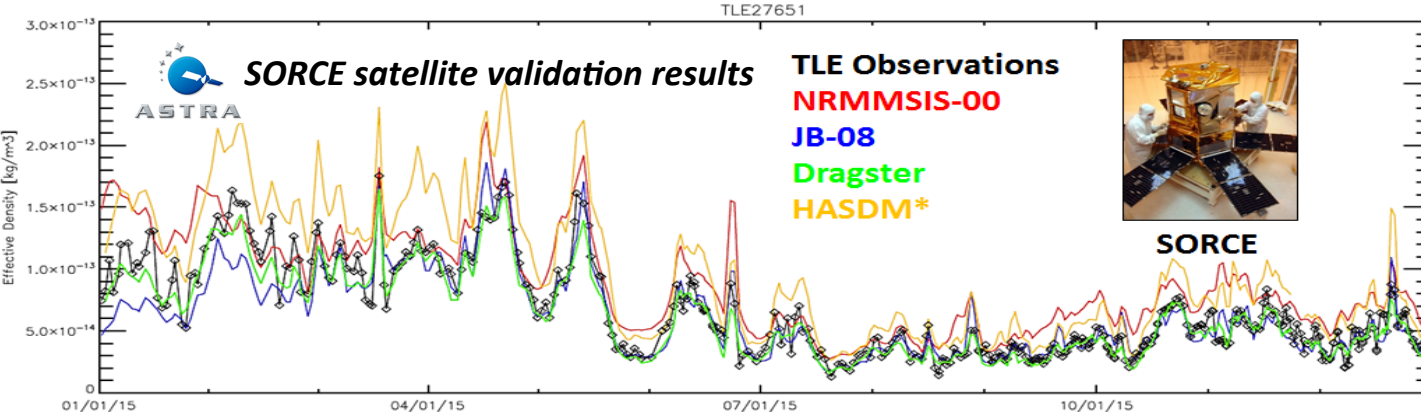
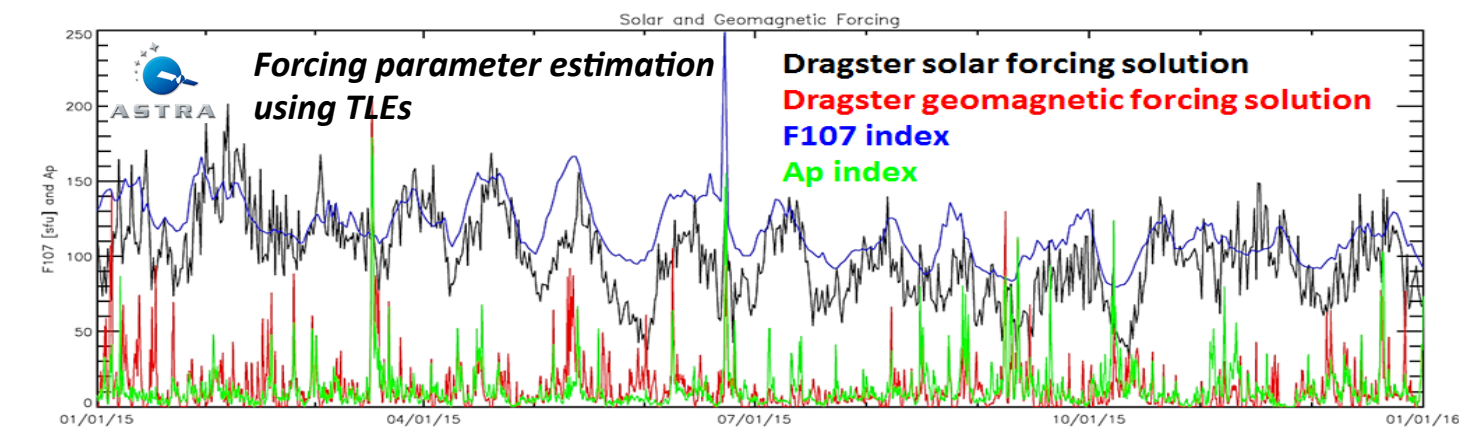
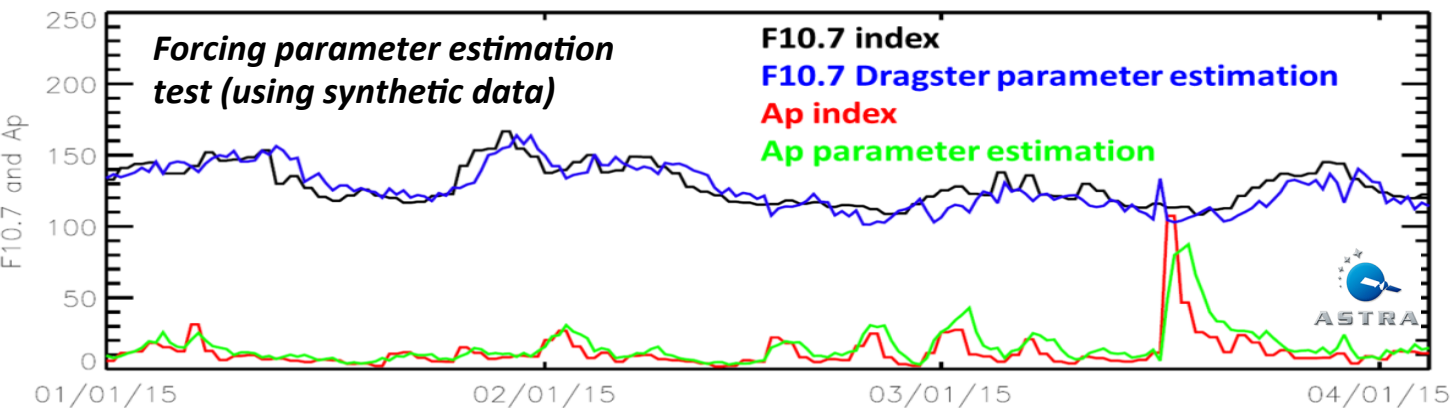
Bowman and Storz 2003

Iterative Re-Initialization, Driver Estimation & Assimilation (IRIDEA)



- Assimilation using accelerometer data and TIE-GCM model
- Uses very small ensembles
- For more (and more up to date) information see **Sutton 2018**

Dragster ENKF-based Technique

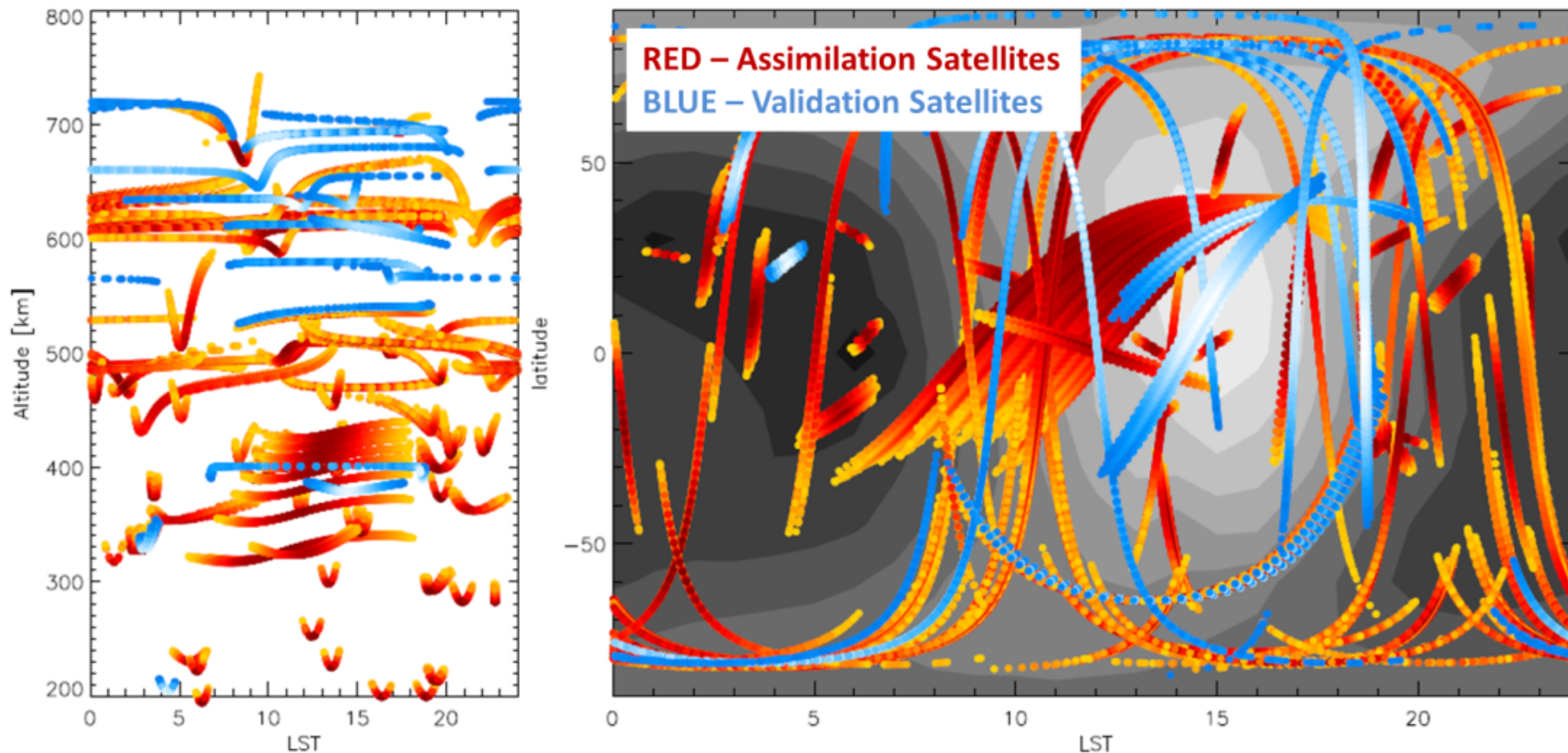


- Developed by ASTRA LLC. as part of AF funded STTR (CU is the educational partner)
- Uses 70-90 assimilation objects and processes satellites with variable ballistic coefficients
- Uses 30-90 ensemble members of NRLMSISE-00, TIE-GCM, and other models
- Estimates forcing
- Also estimates density corrections on a global grid at several altitudes
- Results shown assimilated TLE data (courtesy of ASTRA LLC.)
- For more information see **Pilinski et al. 2016 (AMOS technical paper)**

Assimilating Satellite Drag Data



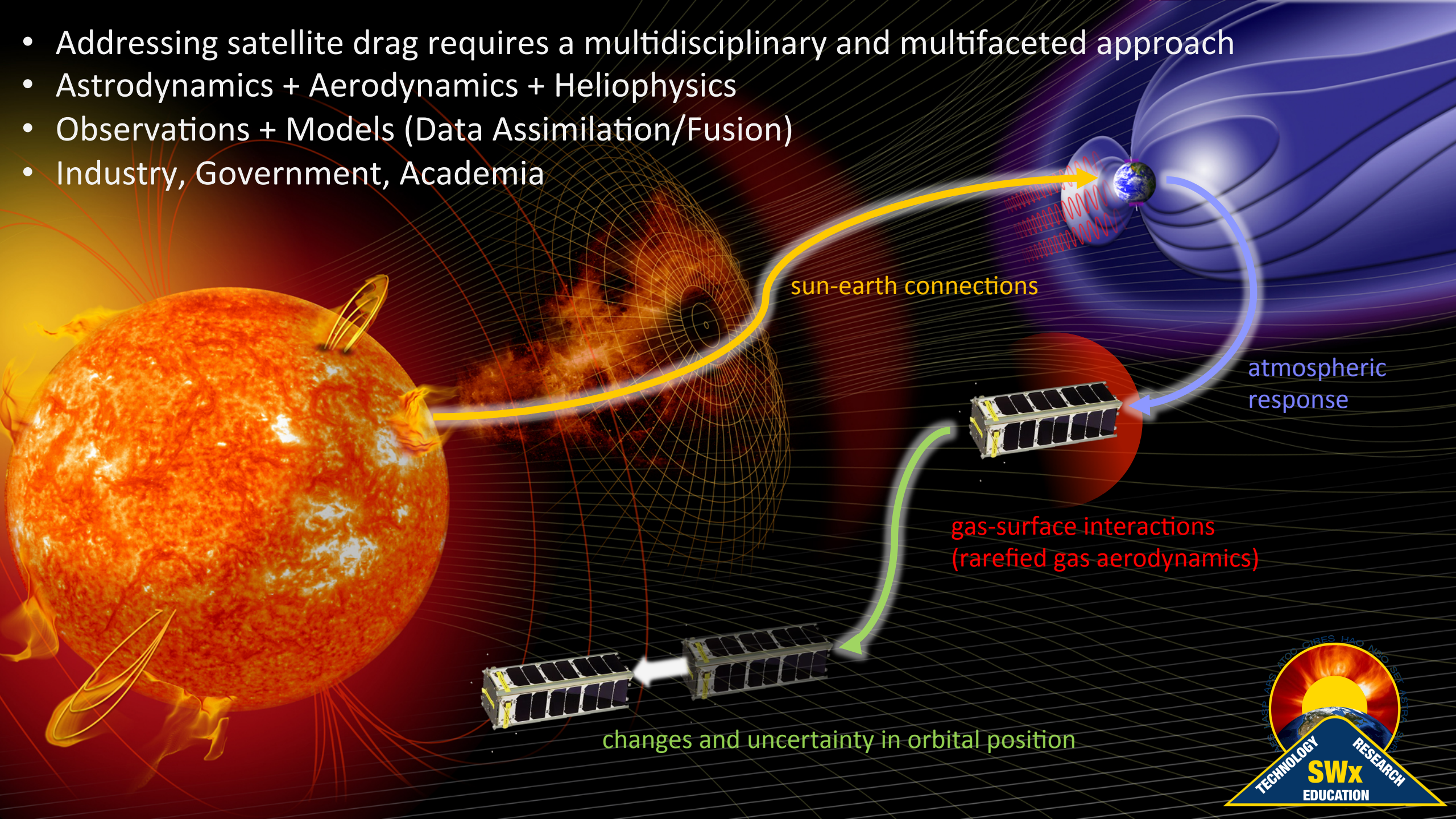
Locations of 90% EDR for a set of assimilation and validation satellites



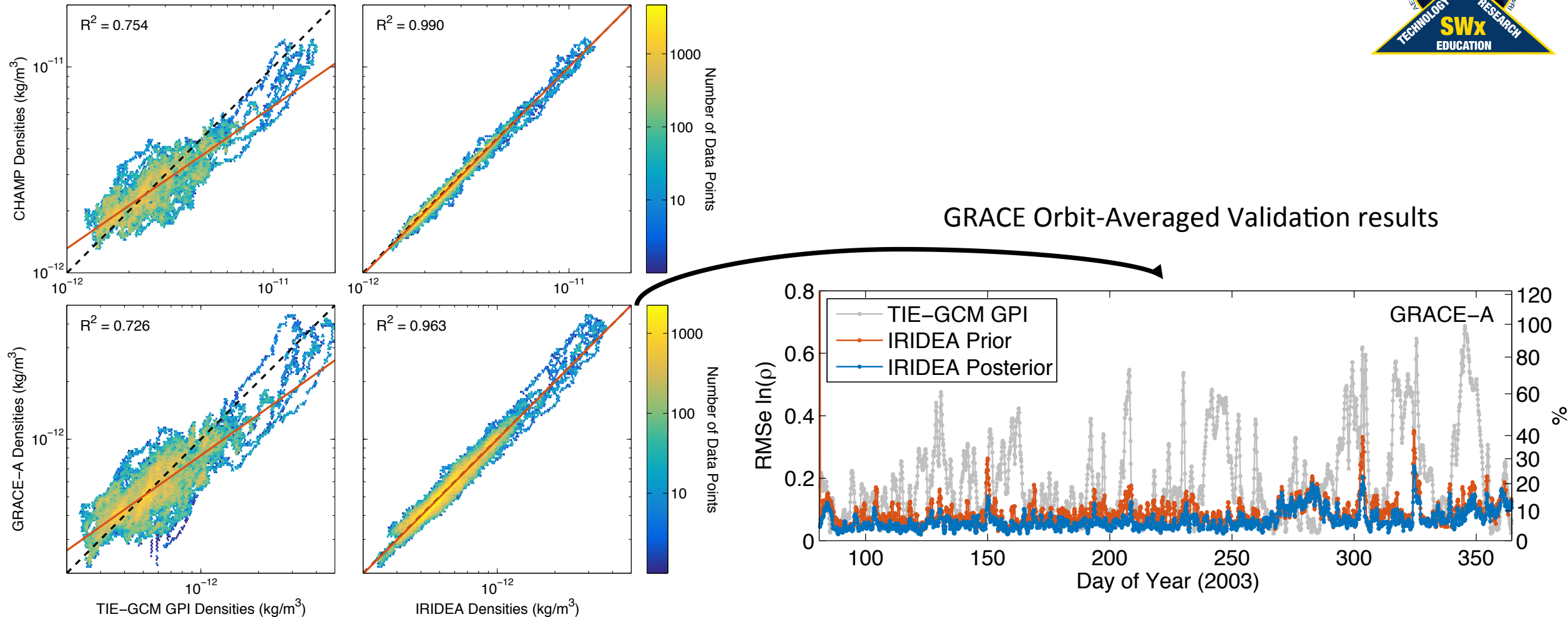
- Example from Dragster assimilation locations and density field at 400 km
- All drag is localized to some extent



- Addressing satellite drag requires a multidisciplinary and multifaceted approach
- Astrodynamics + Aerodynamics + Heliophysics
- Observations + Models (Data Assimilation/Fusion)
- Industry, Government, Academia

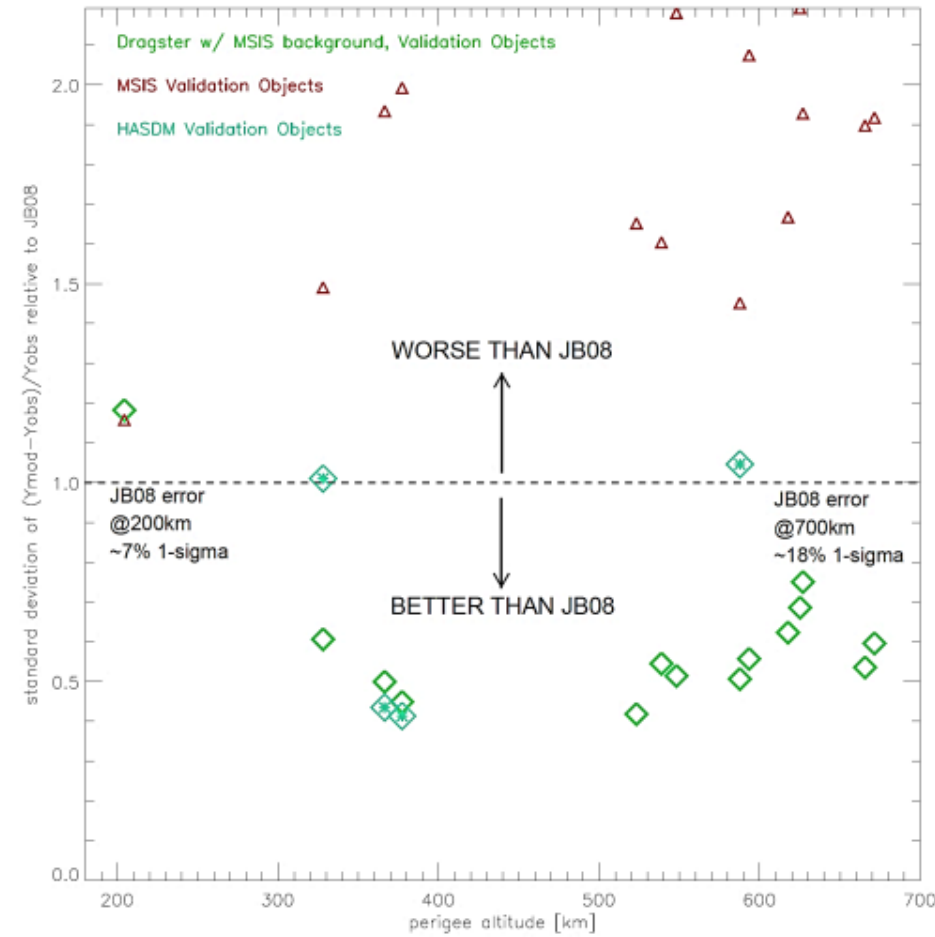


IRIDEA: Backup Slides



[Sutton 2018] Histograms comparing orbit-averaged CHAMP (top) and GRACE-A (bottom) data with TIE-GCM (left) and IRIDEA (right) model output. An orbital running average has been applied to both data and model output prior to binning while the the original output can be seen in Figure S5 of the supporting information. Note: IRIDEA has only ingested the CHAMP data, while the GRACE-A data shown in the bottom plots are used strictly as an independent validation source.

Backup Slides



Standard deviation errors for all validation objects relative to JB08 standard deviations. Values above the dotted line indicate performance worse than JB08 while values below the dotted line indicate performance better than JB08.

2015 validation metrics for select satellites.

Satellite NORAD ID Name (Altitude)	Model ²	Standard Deviation	Bias	Prediction Efficiency
#27651 SORCE (591 km)	M	28%	32%	0.27
	J	20%	-7%	0.53
	H	25%	41%	0.06
	D	15%	-7%	0.68
#40314 Spinsat (390 km)	M	18%	15%	0.30
	J	11%	-12%	0.39
	H	11%	17%	0.33
	D	8%	-11%	0.46
#39267 DANDE (338 km)	M	24%	38%	0.31
	J	14%	10%	0.72
	H	17%	42%	0.10
	D	10%	2%	0.82
#27391 GRACE-A (393 km)	M	19%	31%	-0.08
	J	11%	-0%	0.63
	H	9%	33%	-0.15
	D	7%	0%	0.76

² M-MSIS J-JB08 H-HASDM D-Dragster